

Charge injection and transport in organic semiconductors

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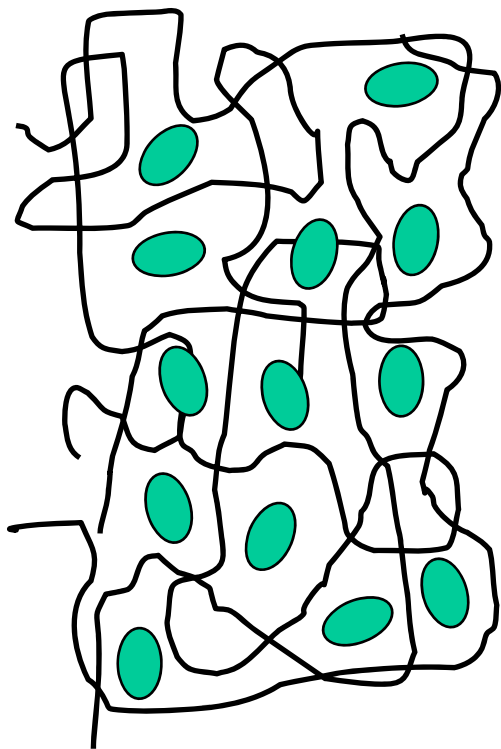
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Cornell NanoScale Science and Technology Facility

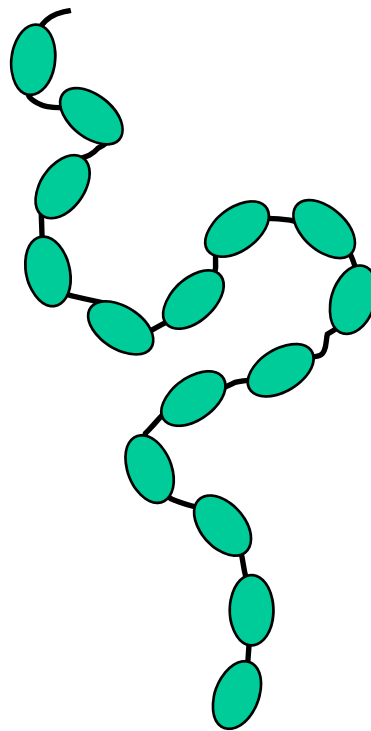
Outline

- Organic semiconductors and devices
- Charge injection and transport processes
- Charge transport in organic semiconductors
- Charge injection in organic semiconductors
- Conclusions

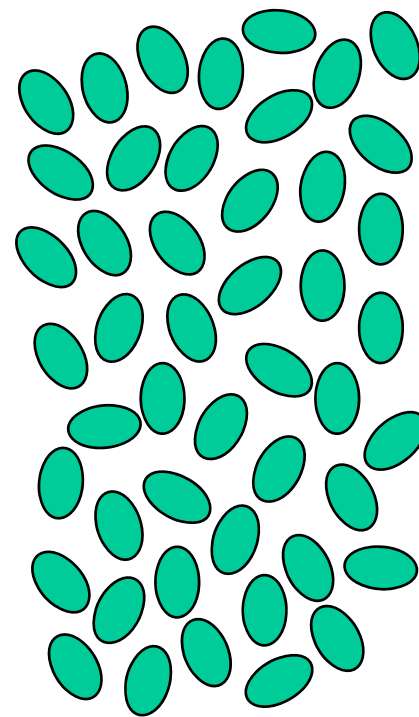
Organic semiconductor families



Molecularly Dispersed
Polymers (MDPs)

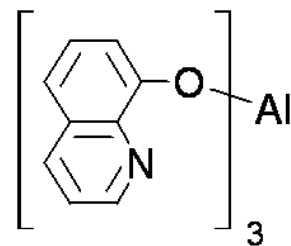
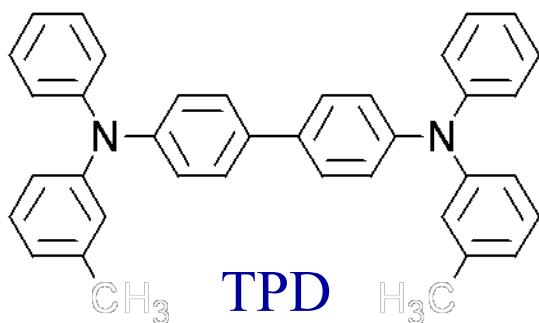


Functional
Polymers

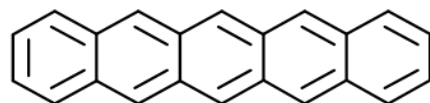


Small Molecules

Examples of conjugated small molecules

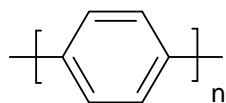


Alq₃

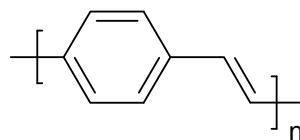


Pentacene

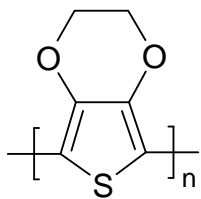
Examples of conjugated polymers



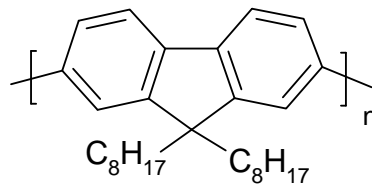
PPP



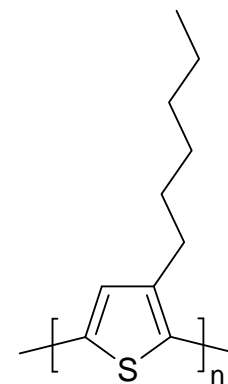
PPV



PEDOT



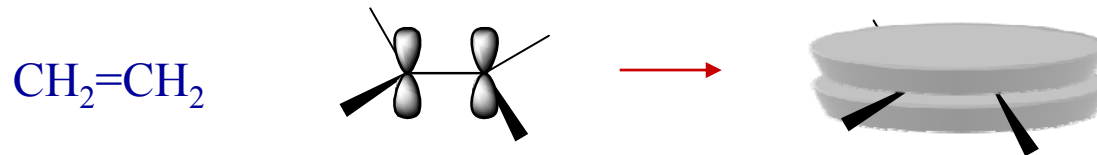
PFO



P3HT

Carbon as a semiconductor

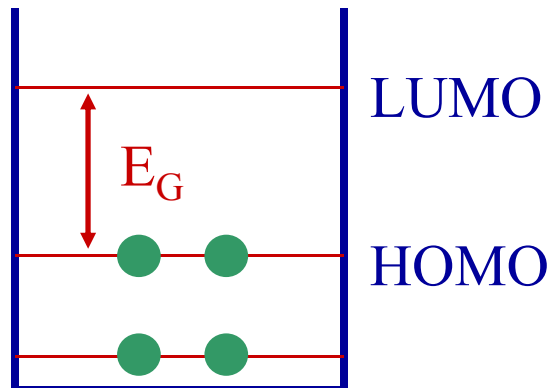
- Hybridization: sp^2 and p_z



- Particle in a box:

$$E_n = \frac{\hbar^2 \pi^2}{2mL^2} n^2$$

$$n=1,2,3,\dots$$



$$E_G \approx \frac{\hbar^2 \pi^2}{2maN}$$

Tuning of optical properties


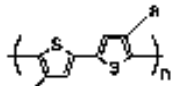

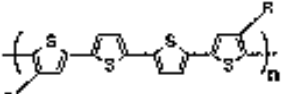
Blue



Red



Table 1. Chemical structures and molecular weight characterization of regio-specific alkylated polythiophenes.

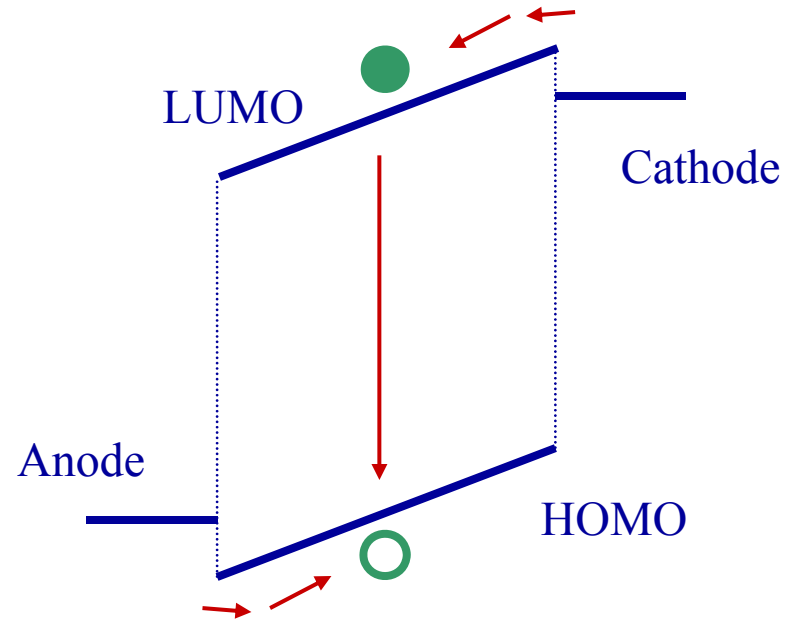
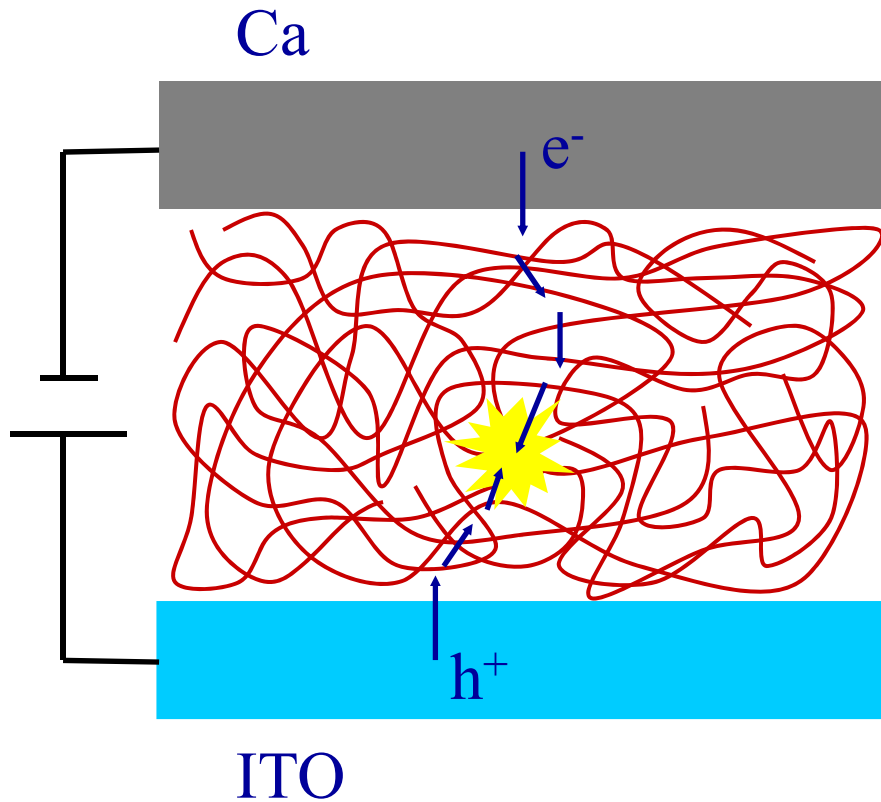
Polymer ^a	$M_n \times 10^{-4}$	M_w/M_n	
	I	1.7	2.3
	II	0.89	1.6
	III	4.2	2.7
	IV	8.5	2.1

[a] R is n-octyl. [b] Relative to polystyrene standards.



Covion

PLED structure and operation



Electroluminescence: charge injection,
charge transport, recombination

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Charge transport in semiconductors

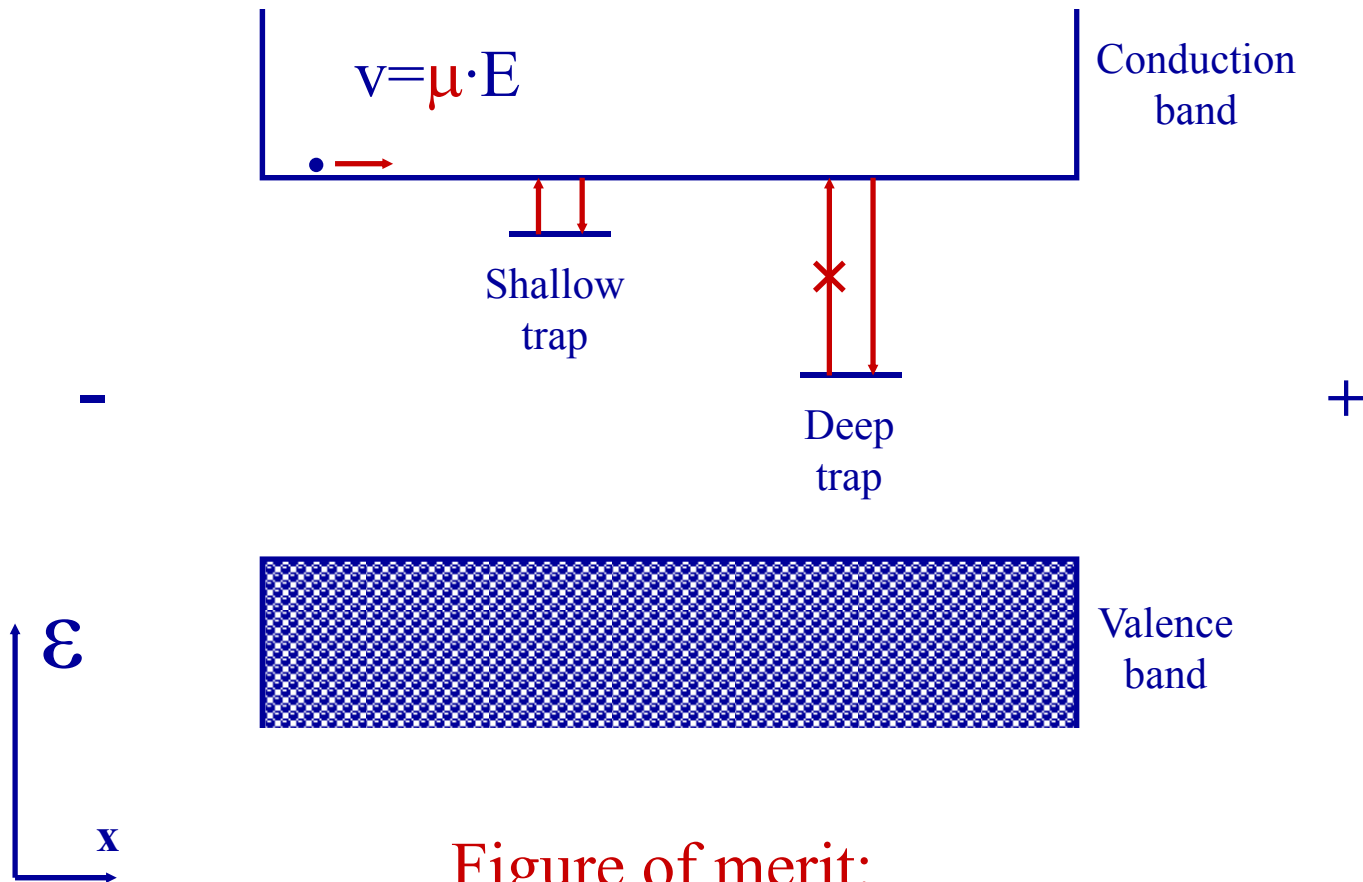
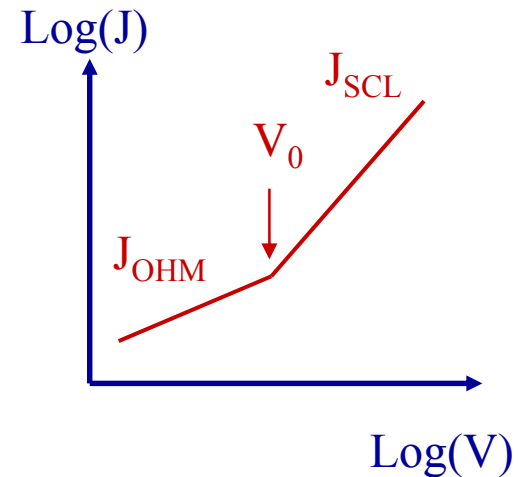
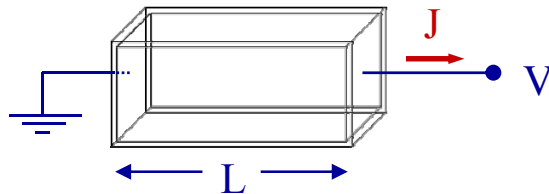


Figure of merit:
mobility, μ ($\text{cm}^2/\text{V}\cdot\text{sec}$)

Charge transport in semiconductors (II)

Question: What is the maximum current that can flow through a (trap-free) semiconductor?



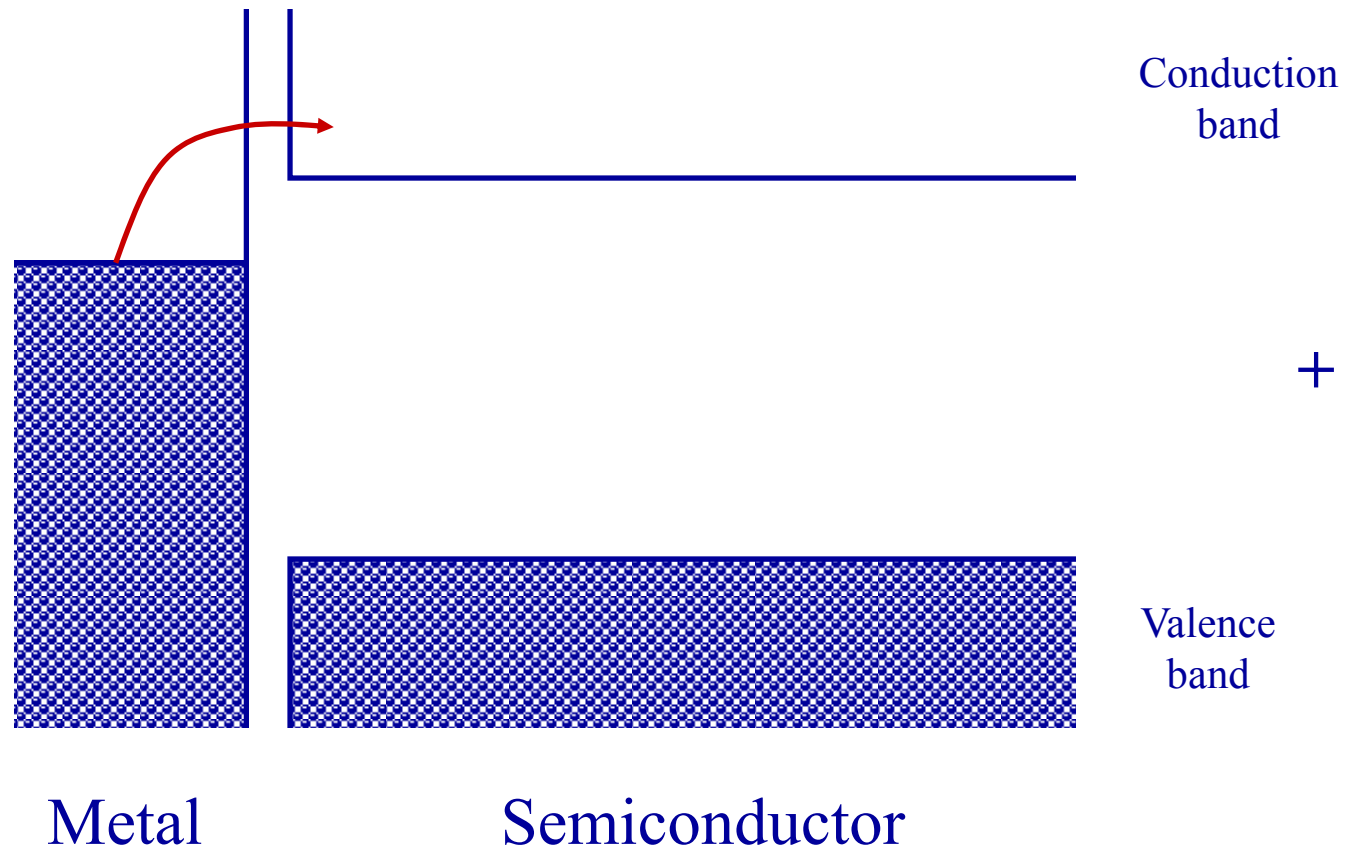
Lower voltages: Ohm's law

$$J_{\text{OHM}} = e \cdot N_0 \cdot \mu \cdot V/L$$

Higher voltages: Space charge limited current

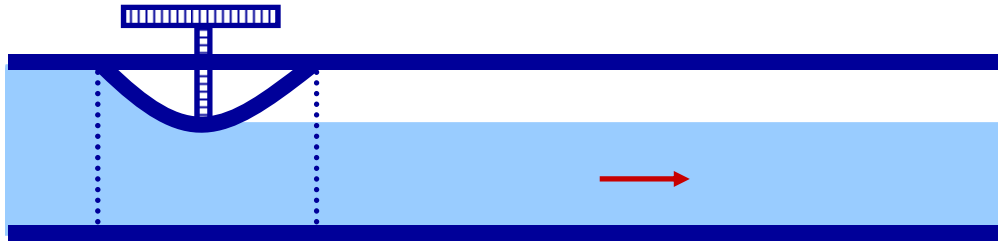
$$J_{\text{SCL}} = (9/8) \cdot \epsilon \cdot \epsilon_0 \cdot \mu \cdot V^2/L^3$$

Charge injection in semiconductors



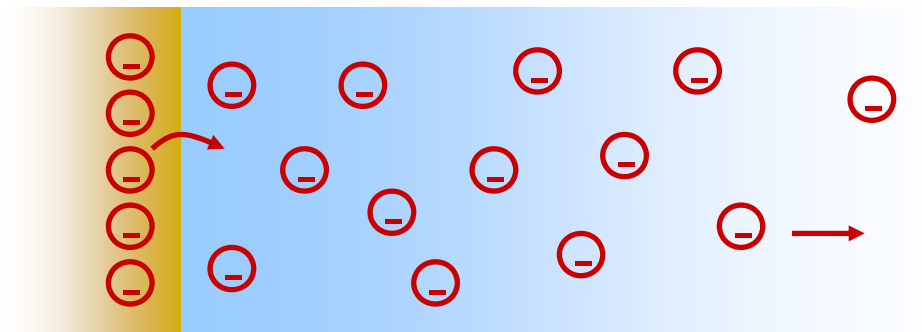
Mechanisms: Thermionic emission or tunneling

Injection vs. transport



Water hose
and valve

Is the flow limited by the valve or the hose?



Semiconductor
contacts

Is the current limited by injection or transport?

Injection vs. transport (II)

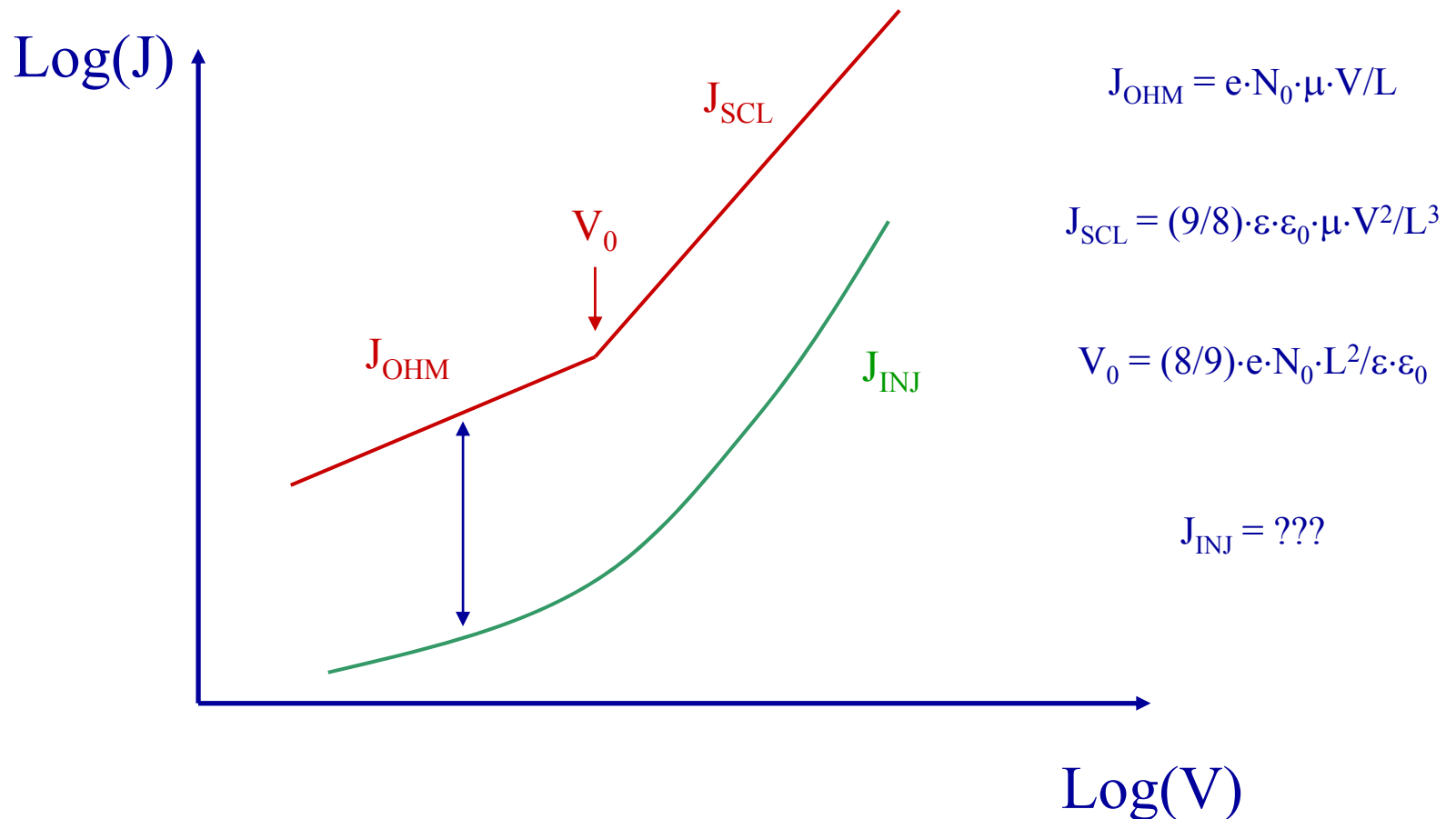
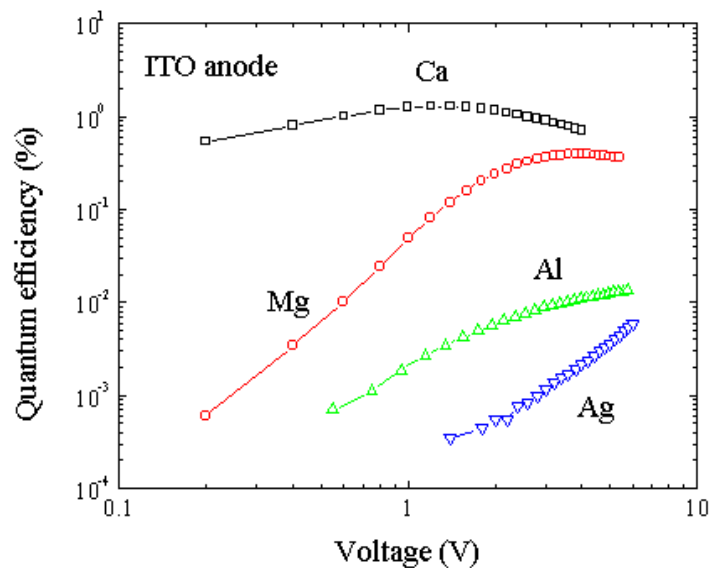
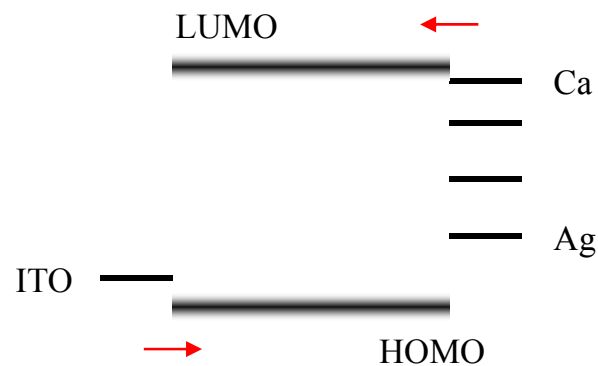
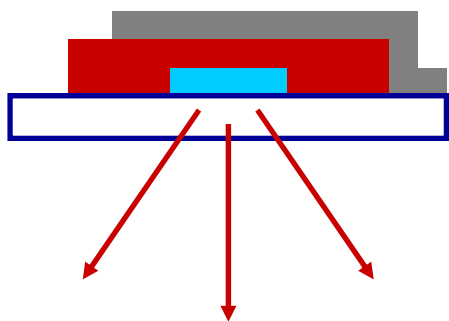
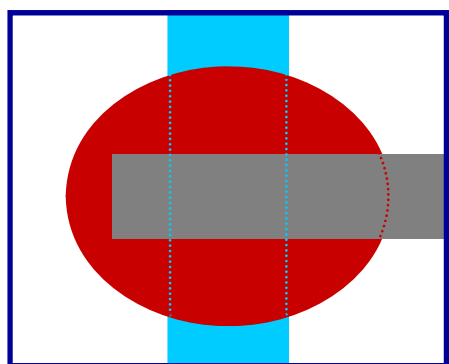


Figure of merit: $\eta = J_{\text{I}NJ} / J_{\text{M}AX}$

Example: Injection-limited performance



Outline

- Organic semiconductors and devices
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- **Charge transport in organic semiconductors**
- Charge injection in organic semiconductors
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Hierarchy of transport models

$$J = e \cdot n \cdot \mu \cdot E + e \cdot D \cdot dn/dx$$

First order correction:

Space charge effects

$$J = (9/8) \cdot \epsilon \cdot \epsilon_0 \cdot \mu \cdot V^2 / L^3$$

Disorder:

Energetics

Influence on mobility

Localized states

$$\mu = \mu(E, T)$$

Manifold filling:

Charge density dependence of mobility

$$\mu = \mu(n)$$

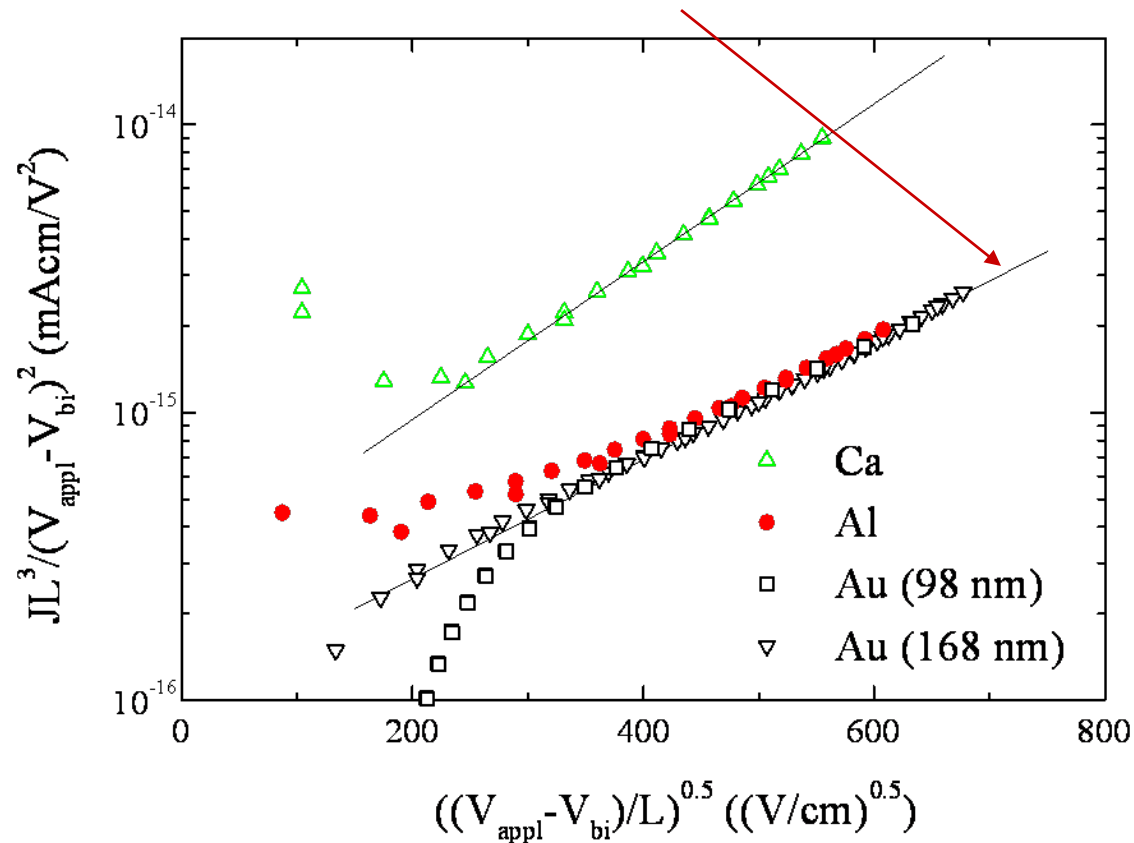
Charge generation:

Electric field dependence of charge density

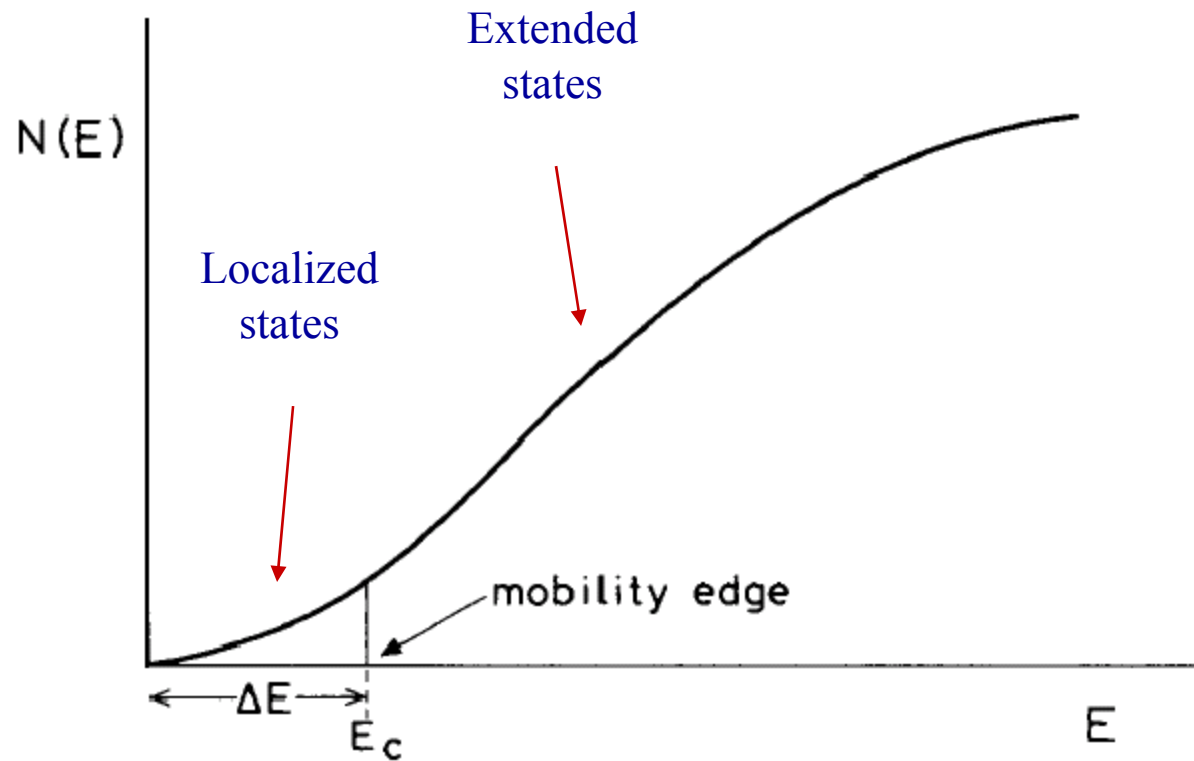
$$n = n(E)$$

Space charge limited current in organics

$$J_{\text{SCL}} \approx (9/8) \epsilon \epsilon_0 \mu_0 V^2 \exp[0.89(V/E_0 L)^{0.5}] / L^3$$

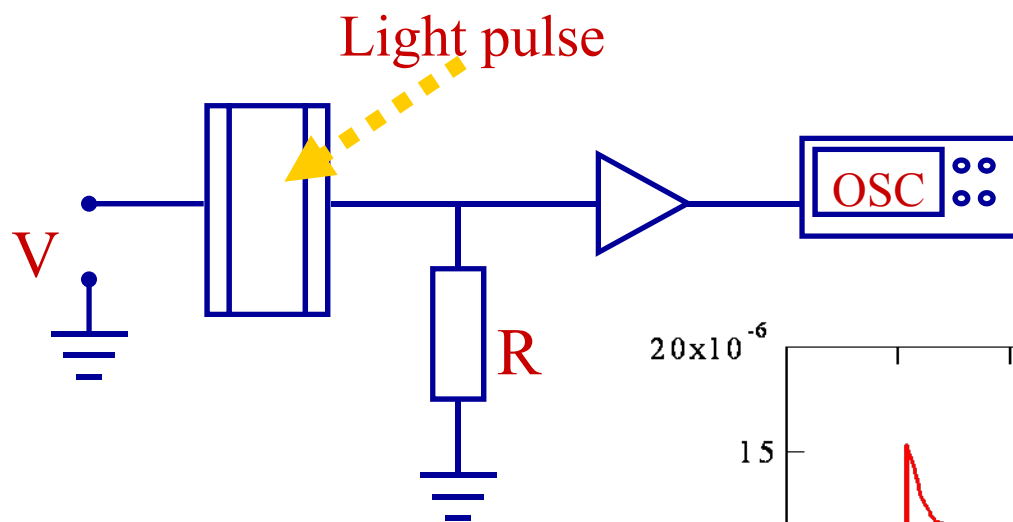


Energetics of amorphous semiconductors

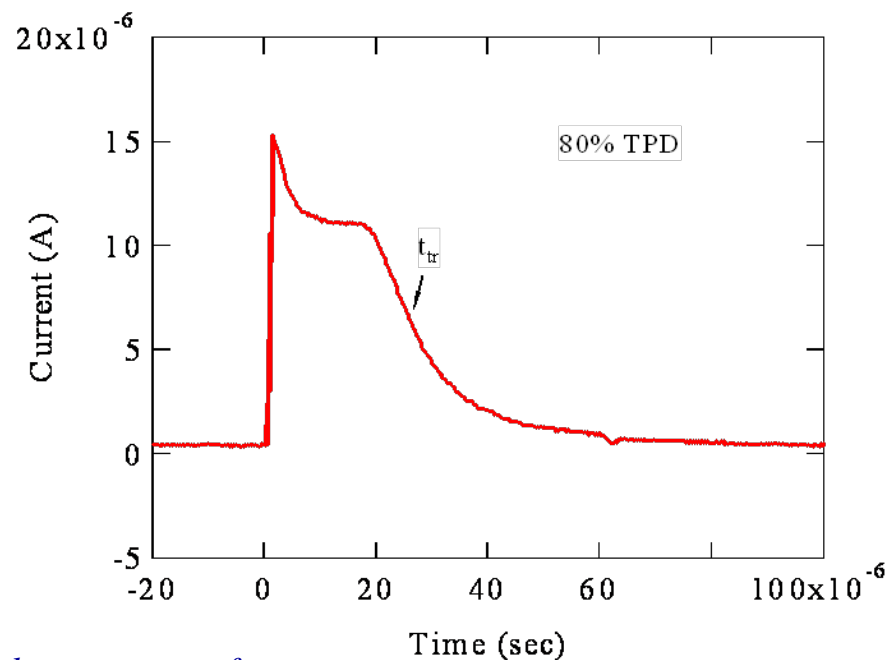


N. Mott, *Nobel Lecture* (1977)

Time-of-flight (TOF)



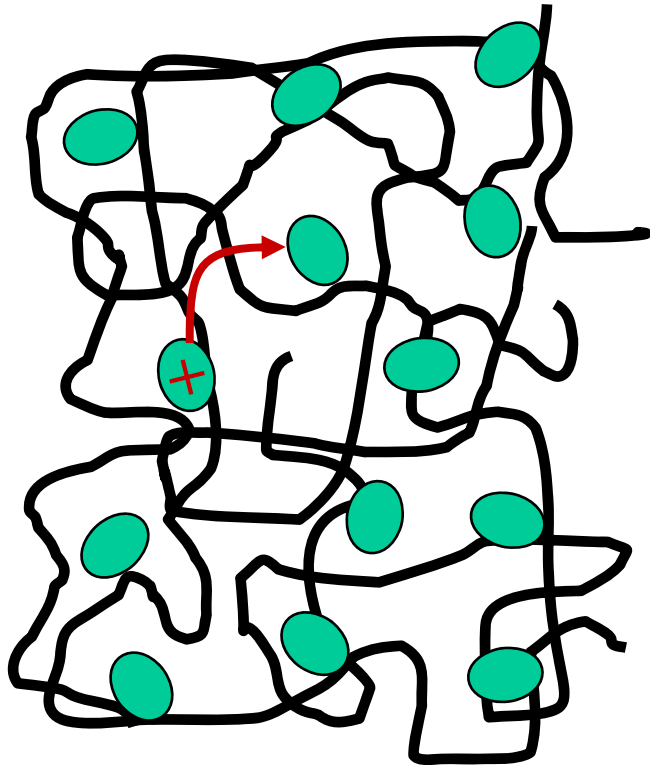
$$\mu = \frac{L^2}{t_{TR} \cdot V}$$



Great book on transport:

P. M. Borsenberger, D. S. Weiss, *Organic photoreceptors for Xerography* (Marcel Decker, Inc., New York, 1998).

Molecularly dispersed polymers

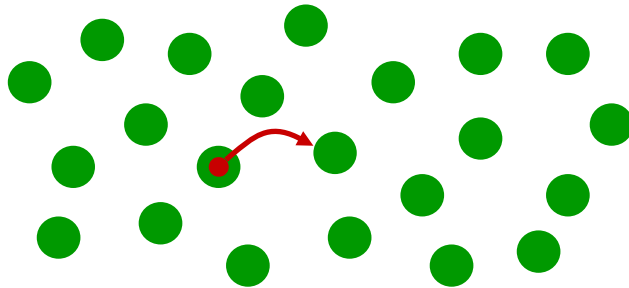
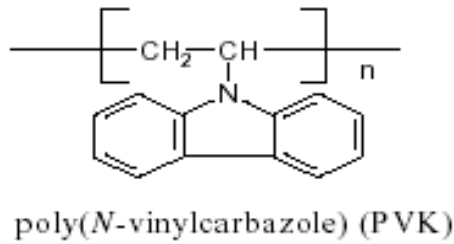


Solid solutions of
conjugated molecules
in inert host

Hopping sites are
well-defined

Control over the
average distance
between hopping sites

Hopping transport



$$v_{ij} \sim \exp(-R_{ij})$$

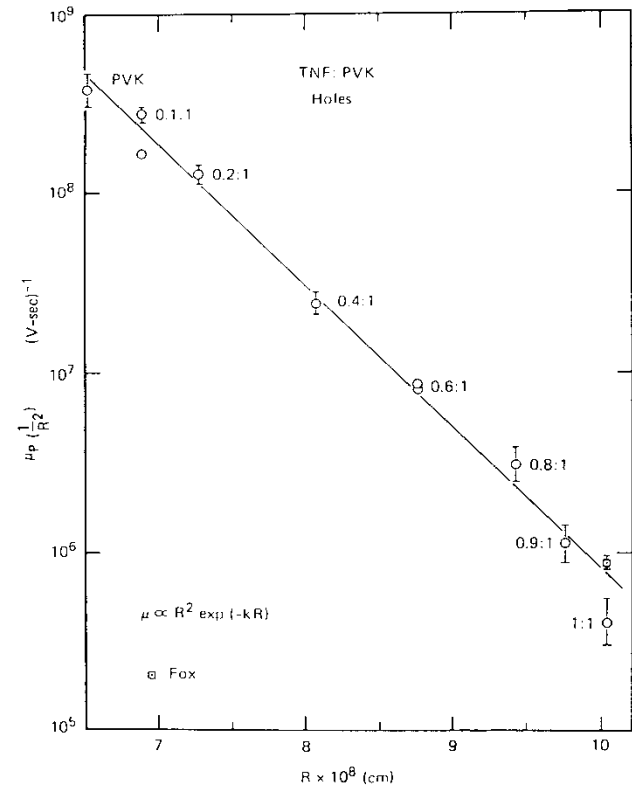
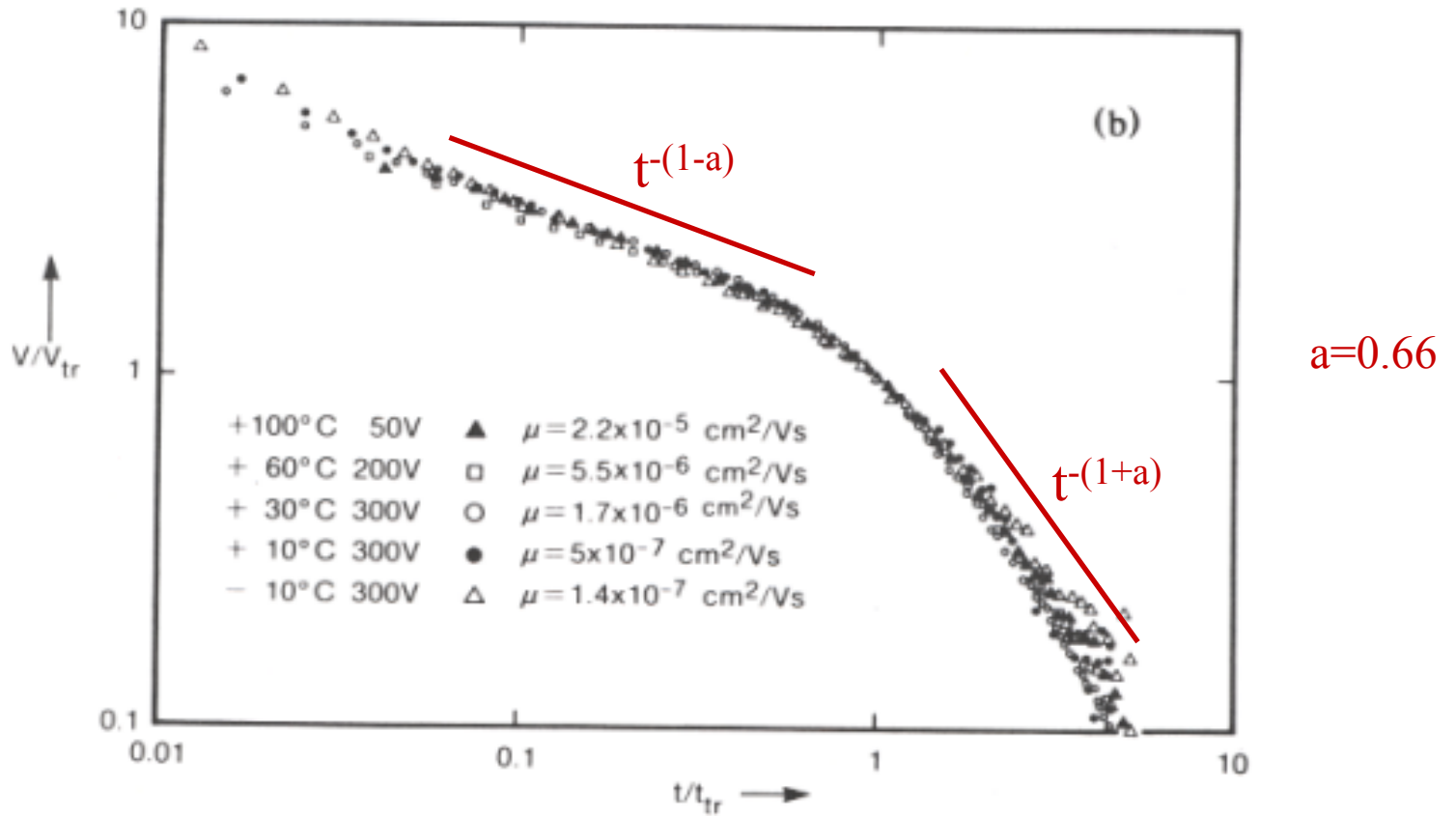
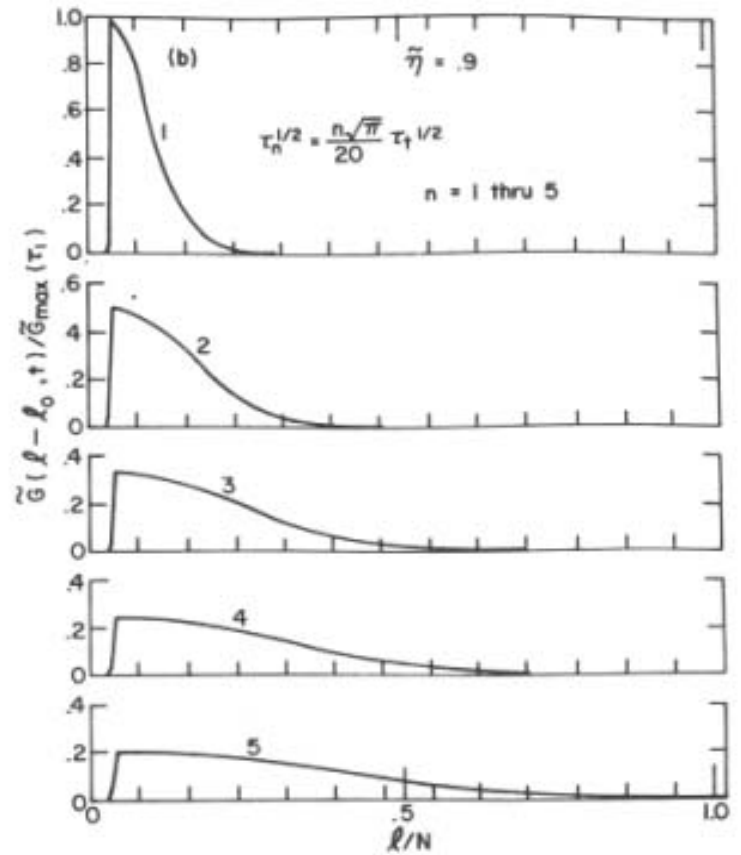
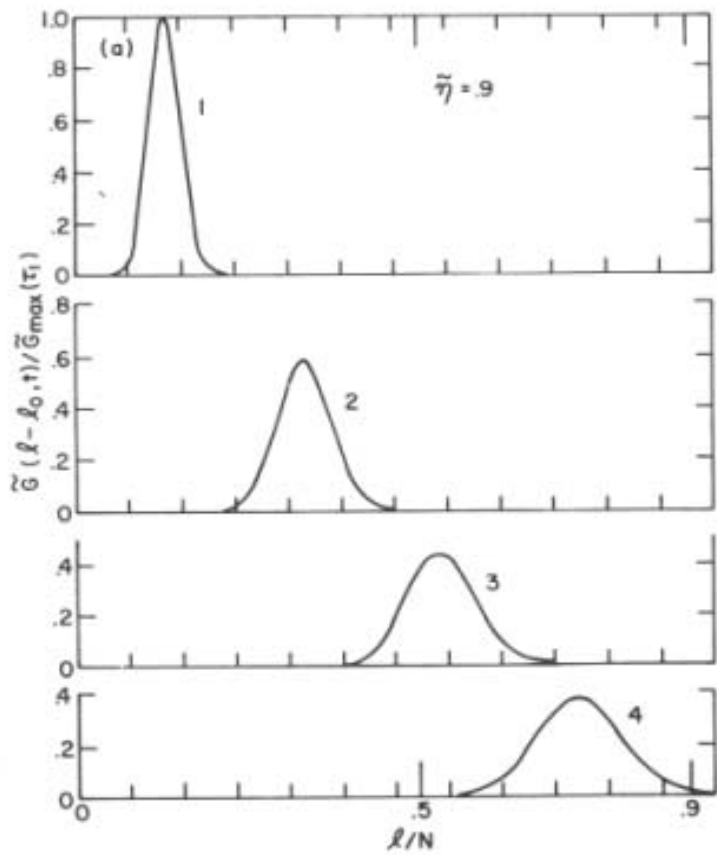


FIG. 9. Hole mobility plotted as a function of the average separation of uncomplexed vinylcarbazole units. A hopping mechanism for hole transport is indicated by the good fit to the functional form of Eq. (3).

Dispersive transport and universality



Disorder formalism (I)



Disorder formalism (II)

Gaussian transport

$$\psi(t) \sim e^{-t/\tau}$$

$$\langle l \rangle \sim t$$

$$\sigma \sim t^{1/2}$$

$$\sigma/\langle l \rangle \sim t^{-1/2}$$

Disorder formalism

$$\psi(t) \sim t^{-(1+a)} \quad (0 < a < 1)$$

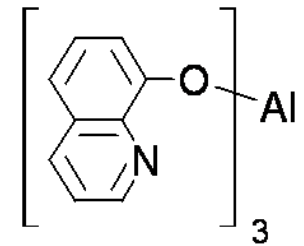
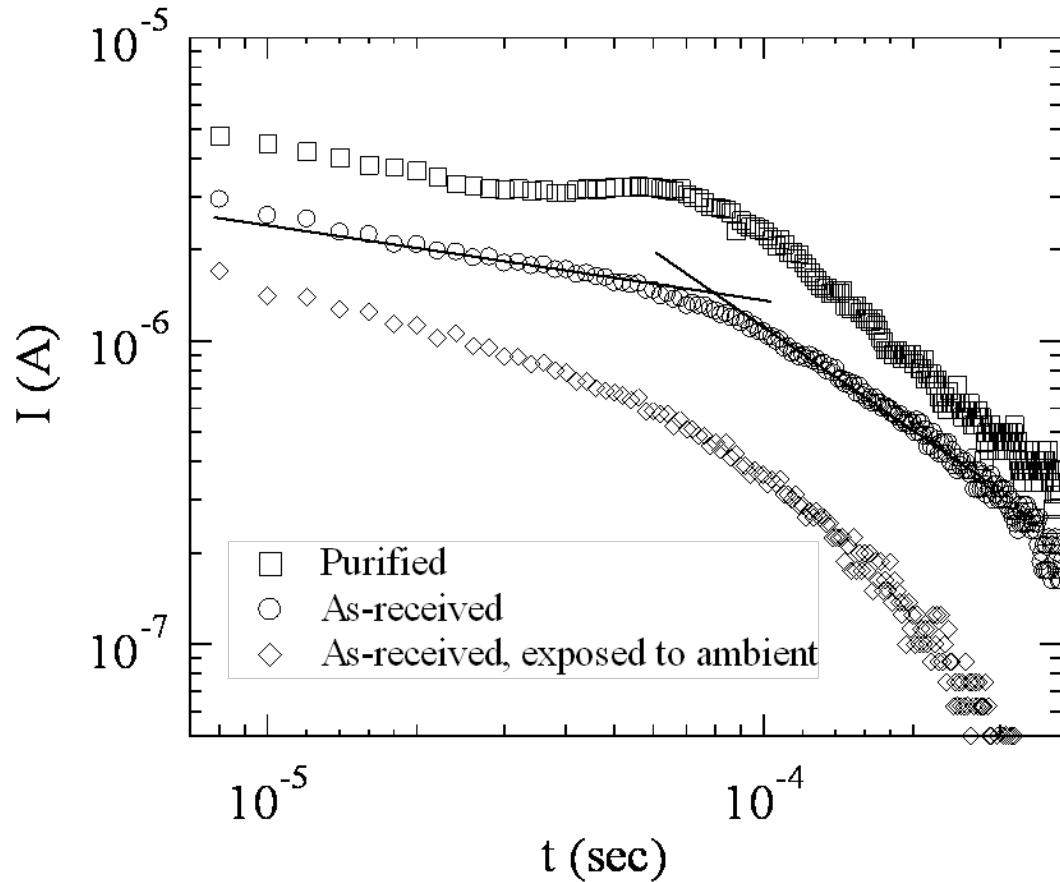
$$\langle l \rangle \sim t^a$$

$$\sigma \sim t^a$$

$$\sigma/\langle l \rangle \sim \text{const.}$$

Universality!

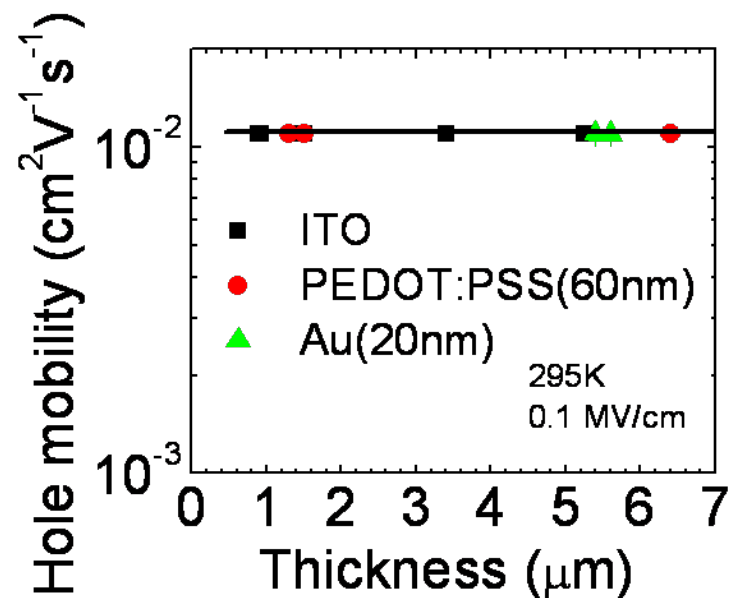
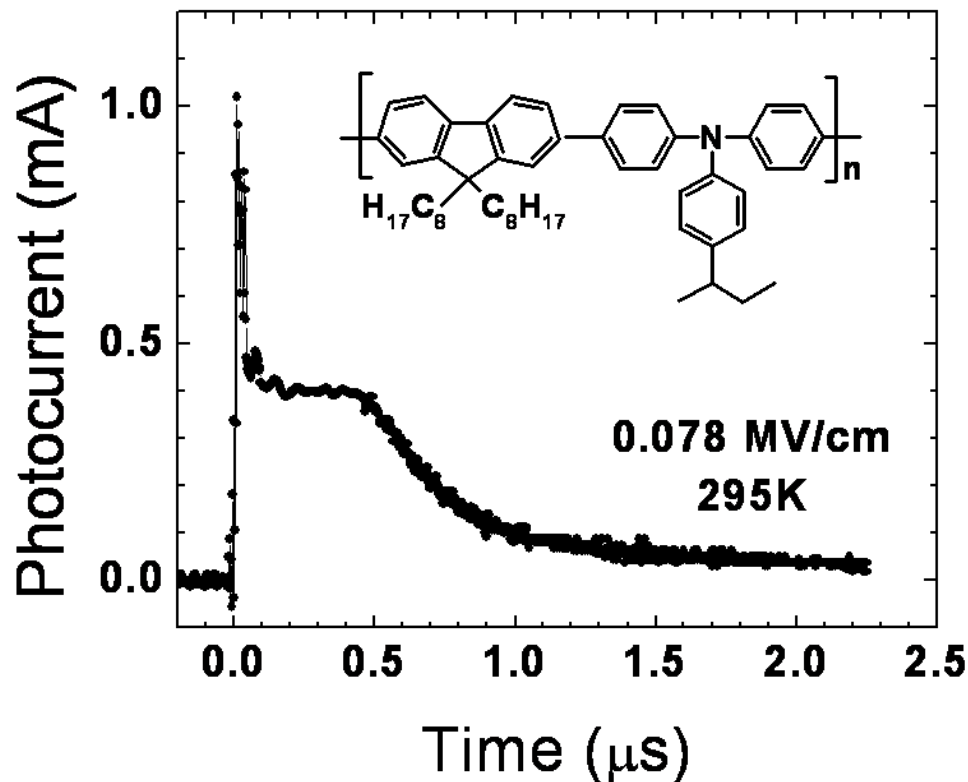
Effect of traps



Alq₃

Non-dispersive hole transport in TFB

ITO/PEDOT:PSS(CH8000)/TFB(6.4 μm)/Al



Transport in MPDs

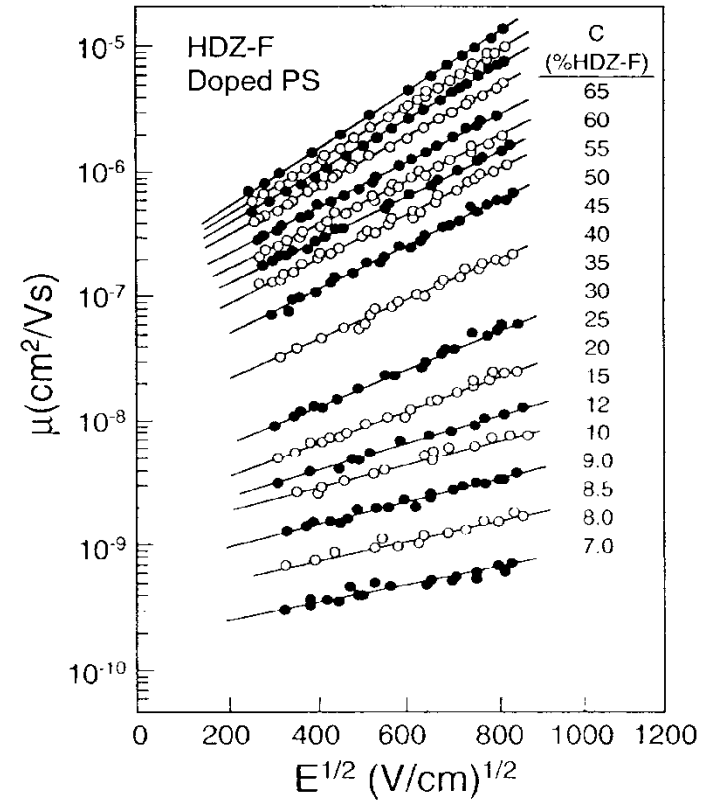
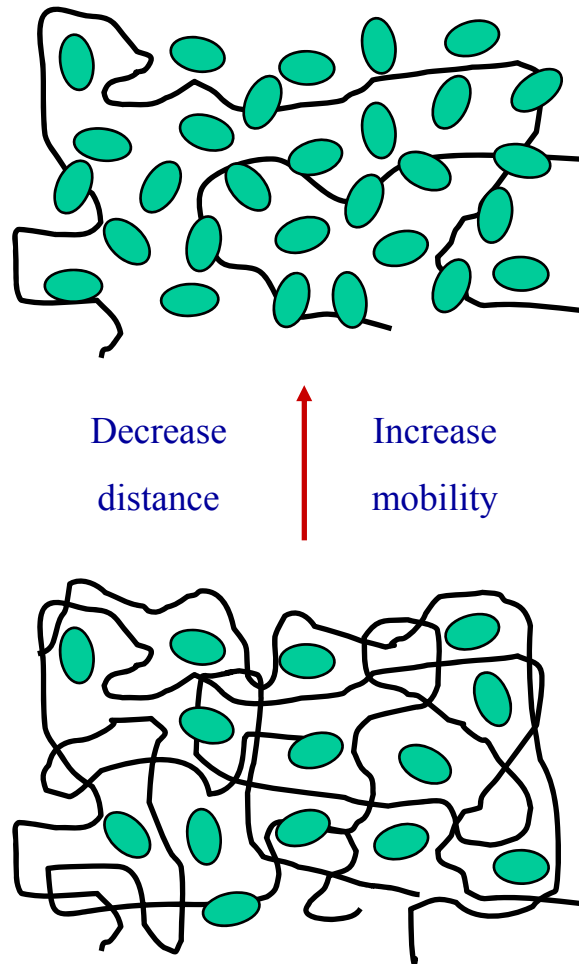
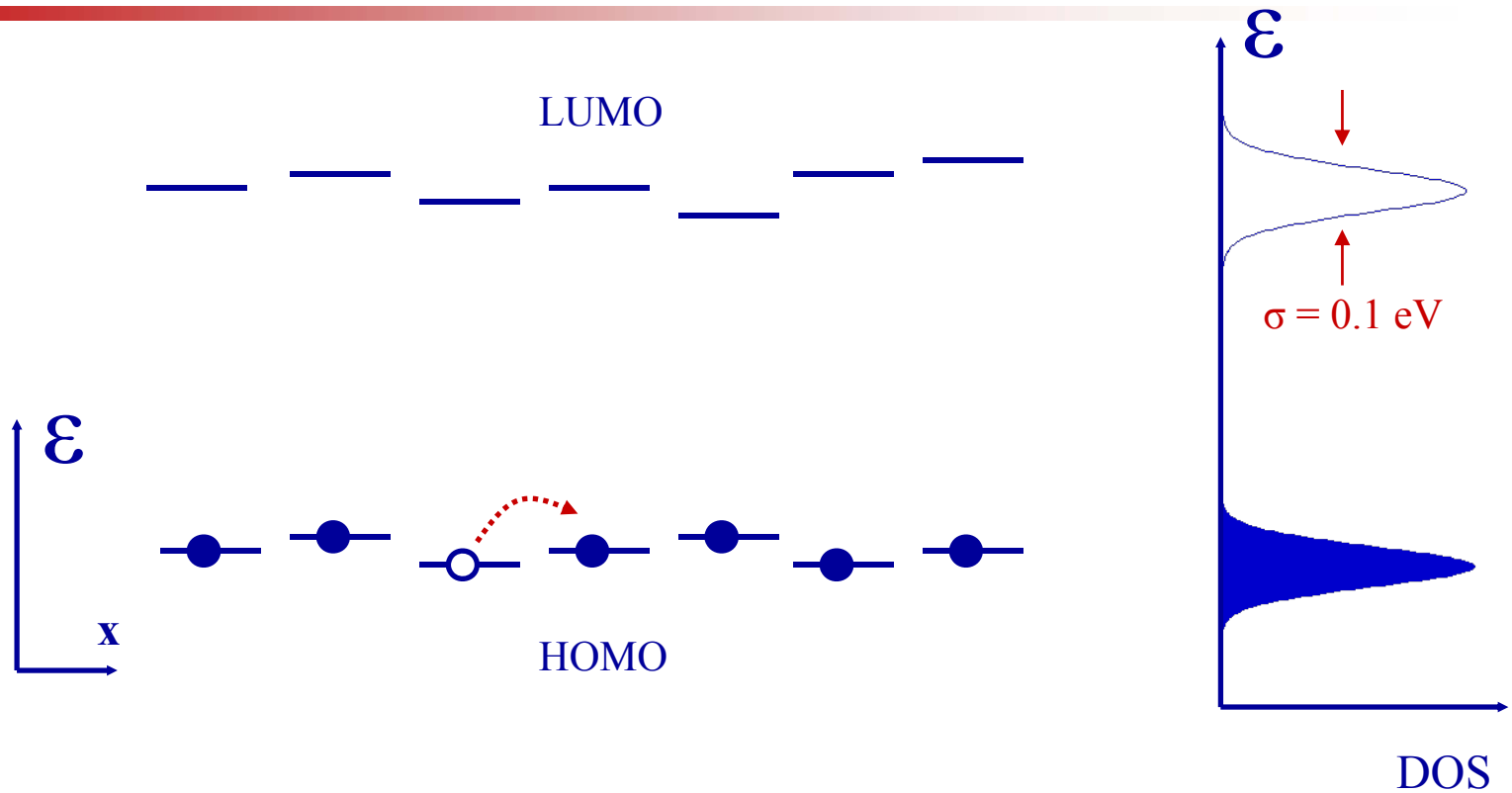


Fig. 2. The field dependencies of the room temperature mobilities for different HDZ-F concentrations.

Gaussian disorder model

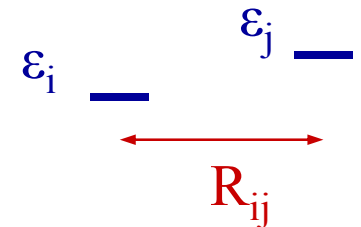


- Energetic disorder
- Positional disorder

Gaussian disorder model (II)

Density of states:

$$\text{DOS}(\varepsilon) = (2 \cdot \pi \cdot \sigma^2)^{-0.5} \cdot \exp[-(\varepsilon^2/2\sigma^2)]$$



Hopping rate:

$$v_{ij} = v_0 \cdot \exp[-(2 \cdot \gamma \cdot a \cdot \Delta R_{ij}/R_{ij})] \cdot \begin{cases} \exp[-(\varepsilon_j - \varepsilon_i)/kT] & ; \varepsilon_j > \varepsilon_i \\ 1 & ; \varepsilon_j < \varepsilon_i \end{cases}$$

Mobility:

$$\mu = \mu_0 \cdot \exp[-(2\sigma/3kT)^2] \cdot \exp\{C \cdot [(\sigma/kT)^2 - \Sigma^2] \cdot E^{0.5}\}$$

Gaussian disorder model (III)

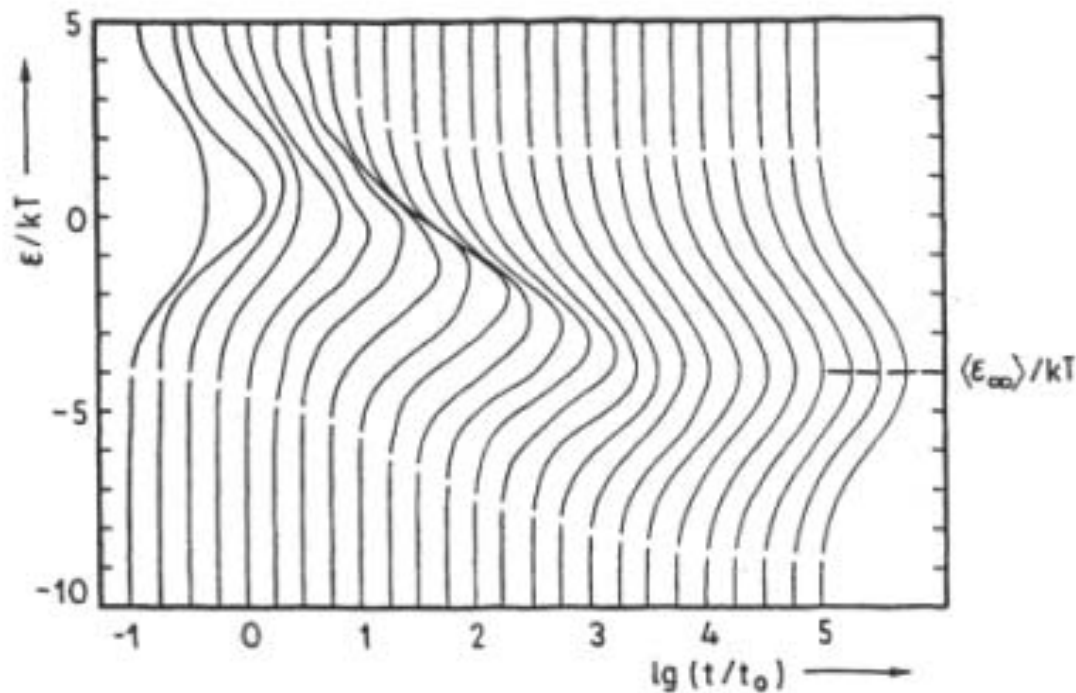


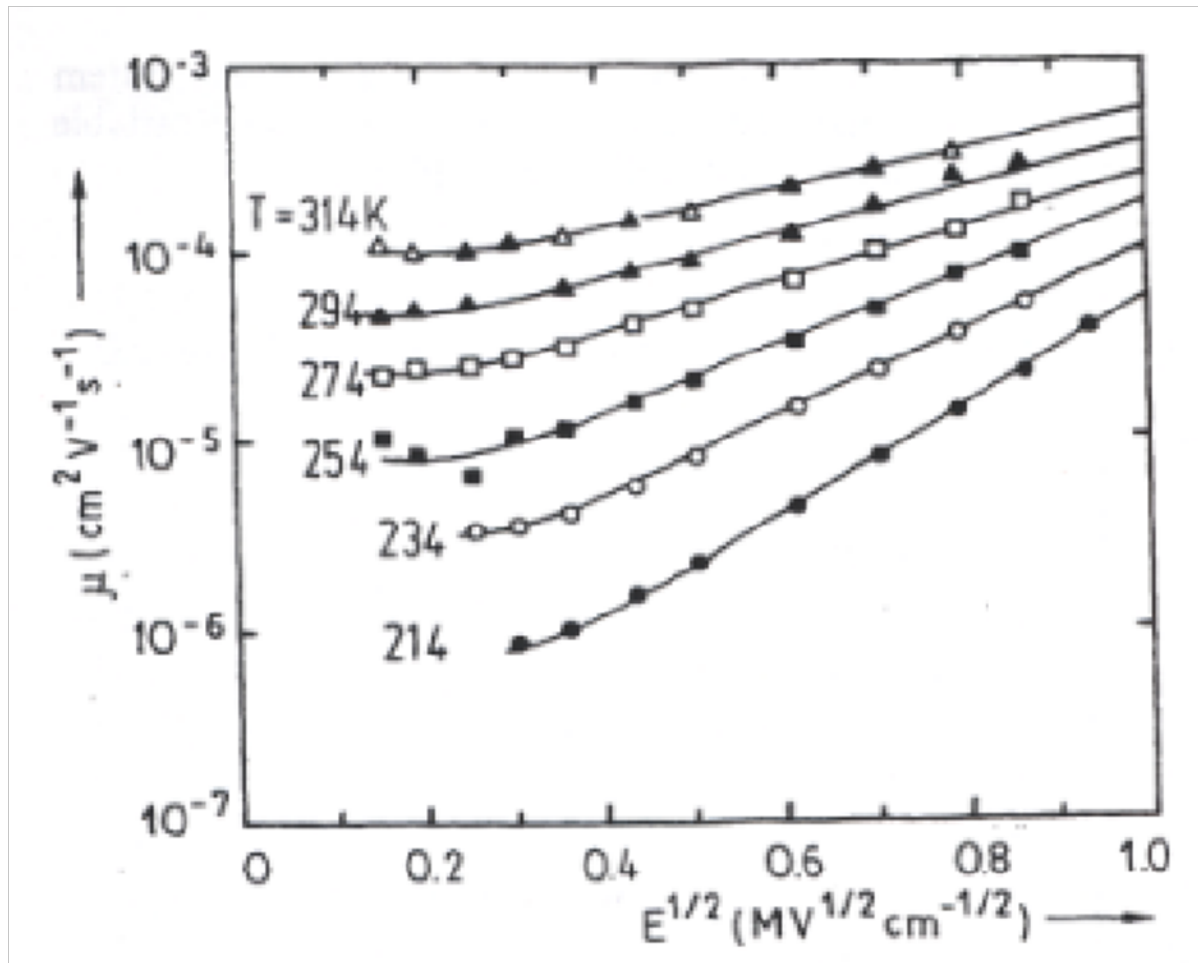
Fig. 2. Temporal evolution of the distribution of carrier energies in a Gaussian DOS of width $\sigma = 2$. All profiles are broken at the same carrier density illustrating the different relaxation patterns for mobile and immobile carriers. ϵ_{∞} denotes the theoretical mean energy in the long-time limit

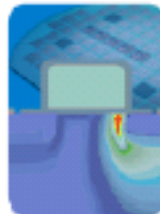
Carriers relax at:

$$\sigma^2/kT$$

$$\mu \sim \exp[-(\sigma/kT)^2]$$

Comparison with experiment



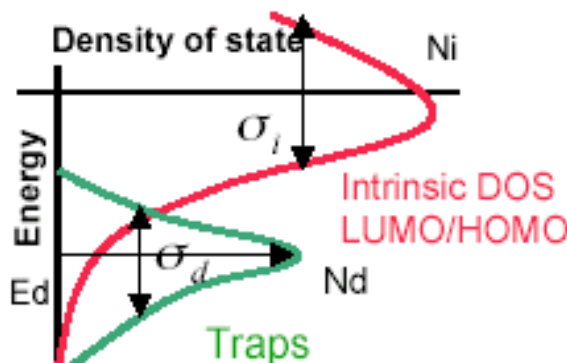


Physical Models for Analysis of Electrical Characteristics for Organic Devices

- Hopping Model

- Effective Transport Energy

- The effective carrier transport energy (E_{tr}) is calculated from^{1,2}:



$$\int_{-\infty}^{E_{tr}} g(E)(E_{tr} - E)^3 dE = \frac{6\beta}{\pi} (\gamma kT)^3$$

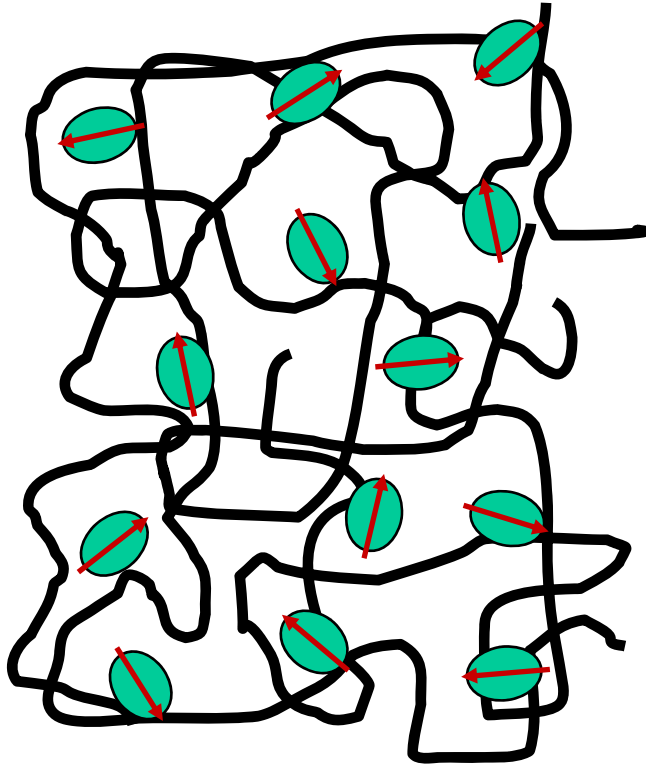
$$g(E) = \frac{N_i}{\sqrt{2\pi}\sigma_i} \exp\left(\frac{-E^2}{2\sigma_i^2}\right) + \frac{N_d}{\sqrt{2\pi}\sigma_d} \exp\left(\frac{-(E + E_d)^2}{2\sigma_d^2}\right)$$

Where $g(E)$ is the DOS distribution, N_i is the total intrinsic state density, N_d is the total dopant state density, σ_i is the intrinsic Gaussian DOS width, σ_d is the dopant Gaussian DOS width, E_d is the energy shift, γ is 1/carrier localization radius, β is the percolation constant, E is the band energy, k is Boltzmann's constant and T is the lattice temperature

¹"Charge carrier mobility in doped disordered organic semiconductors" - V.I. Arkhipov, P. Heremans, E.V. Emelianova, G.J. Adriaenssens, H. Bassler, Journal of Non-Crystalline Solids, 338-340, pp 603-603, 2004.

²"Charge carrier mobility in doped semiconducting polymers" - V.I. Arkhipov, P. Heremans, E.V. Emelianova, G.J. Adriaenssens, H. Bassler, Applied Physics Letters, Vol. 82, No. 19, pp 3245-3247, 2003.

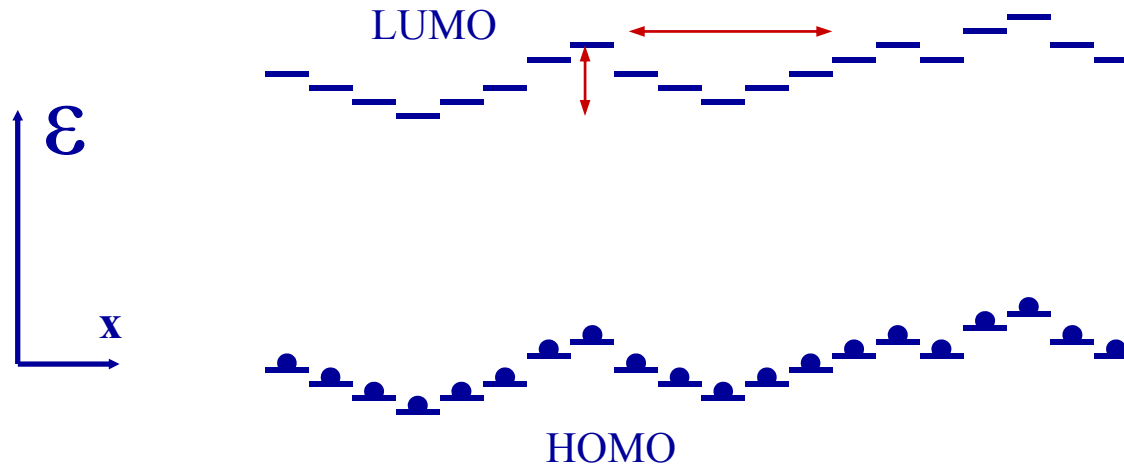
Correlated disorder (I)



Molecules carry a large dipole moment.

Charge dipole interaction causes spatial correlation in the energy of hopping sites.

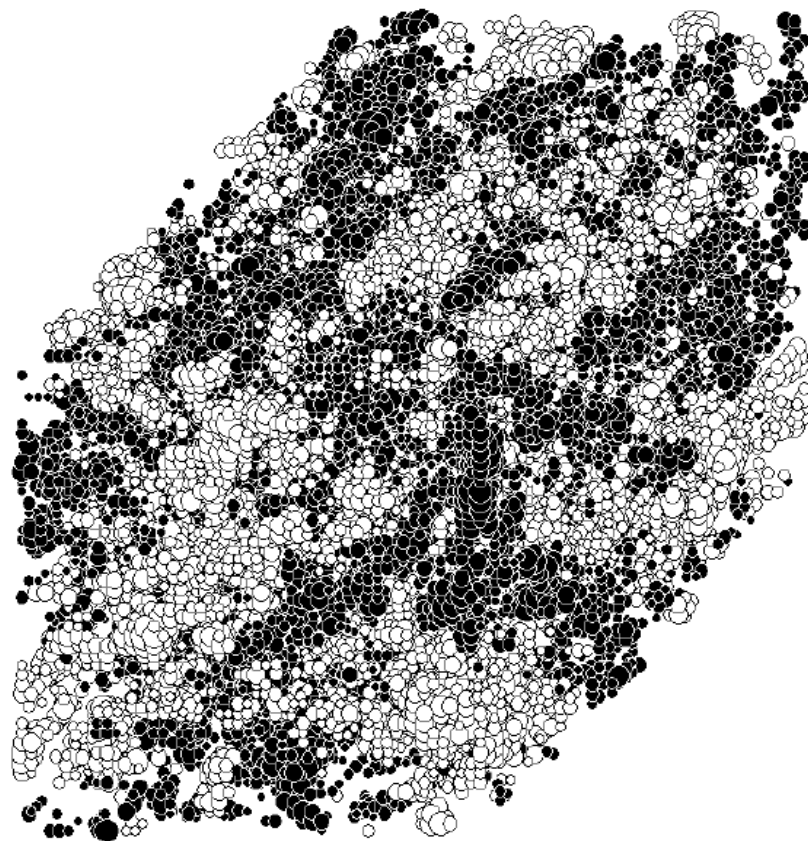
Correlated disorder (II)



Deeper valleys are also wider.

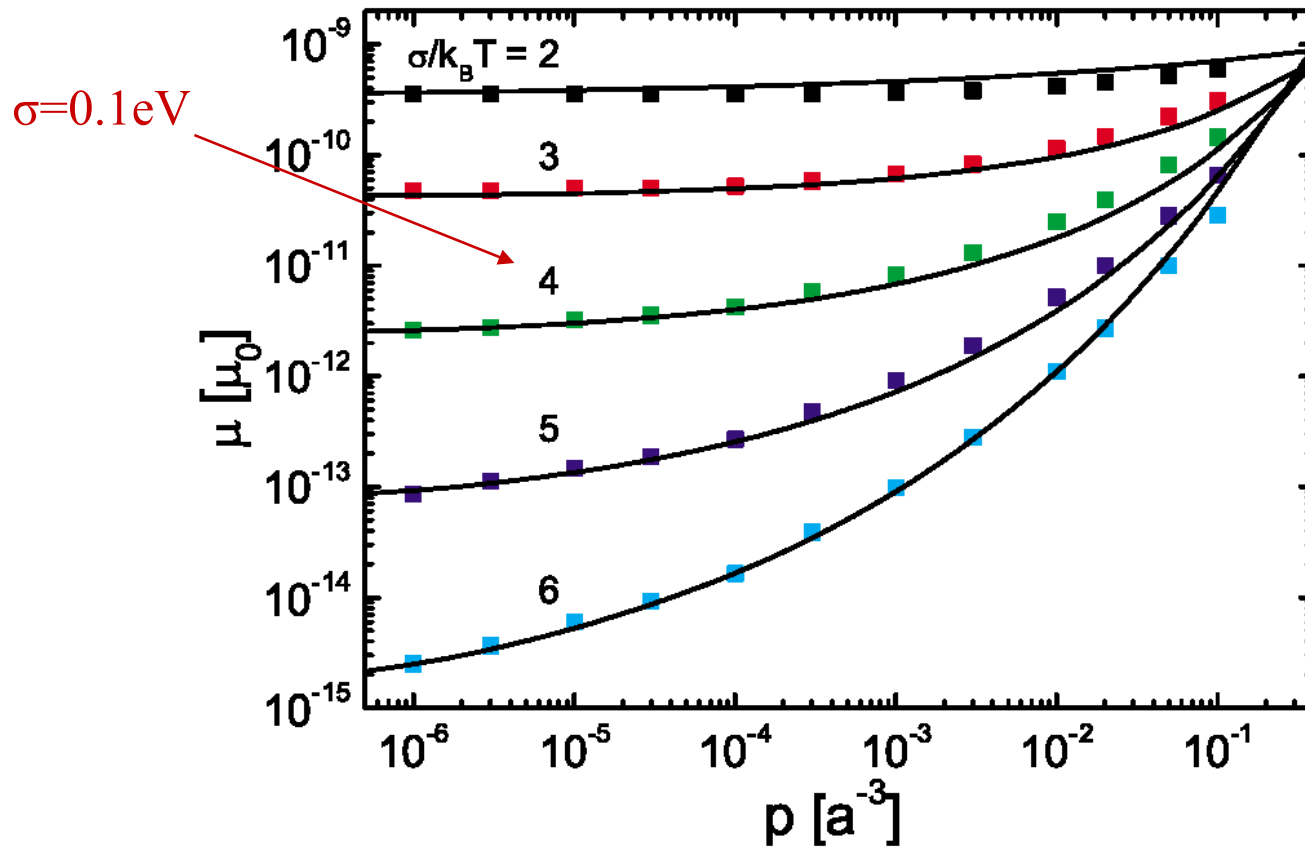
$$\mu = \mu_0 \cdot \exp[-(\sigma/kT)^2 + 2 \cdot (\sigma/kT) \cdot (e \cdot a \cdot E/kT)^{0.5}]$$

Correlated disorder (III)



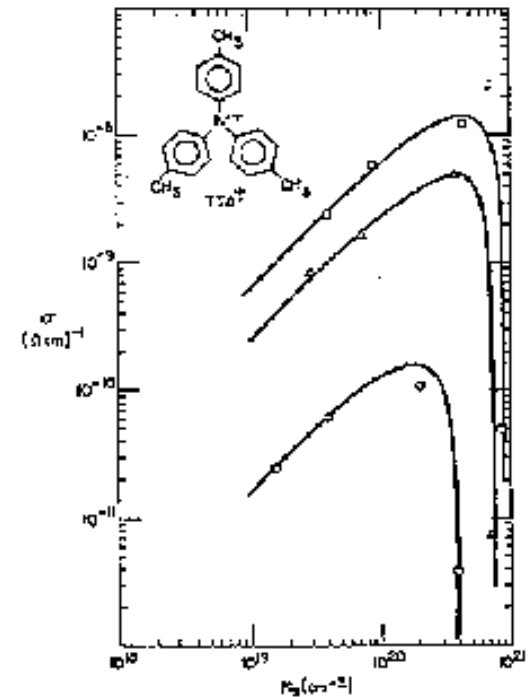
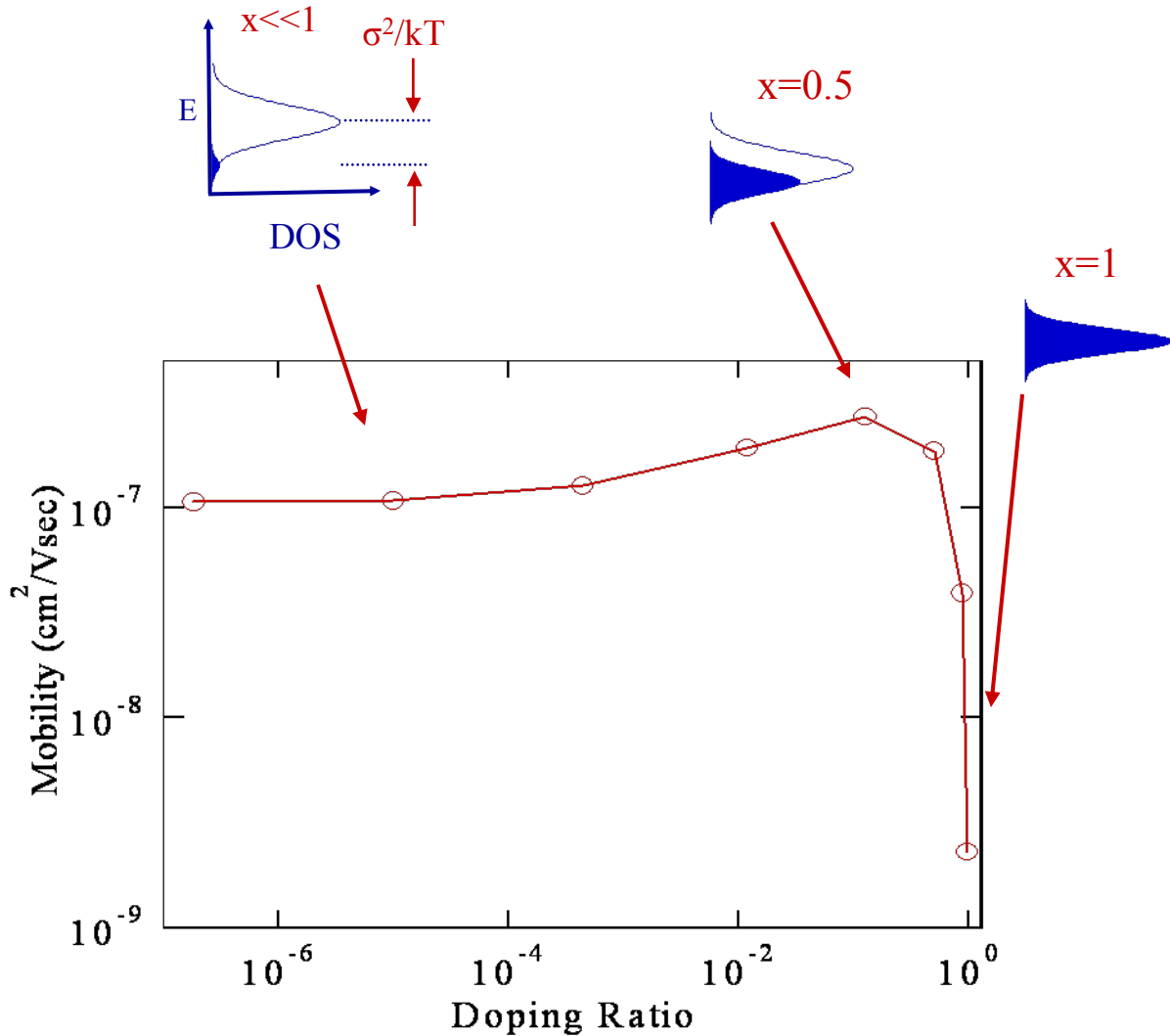
Black/white:
sites with energy
above/below the
mean.

Mobility vs. charge density



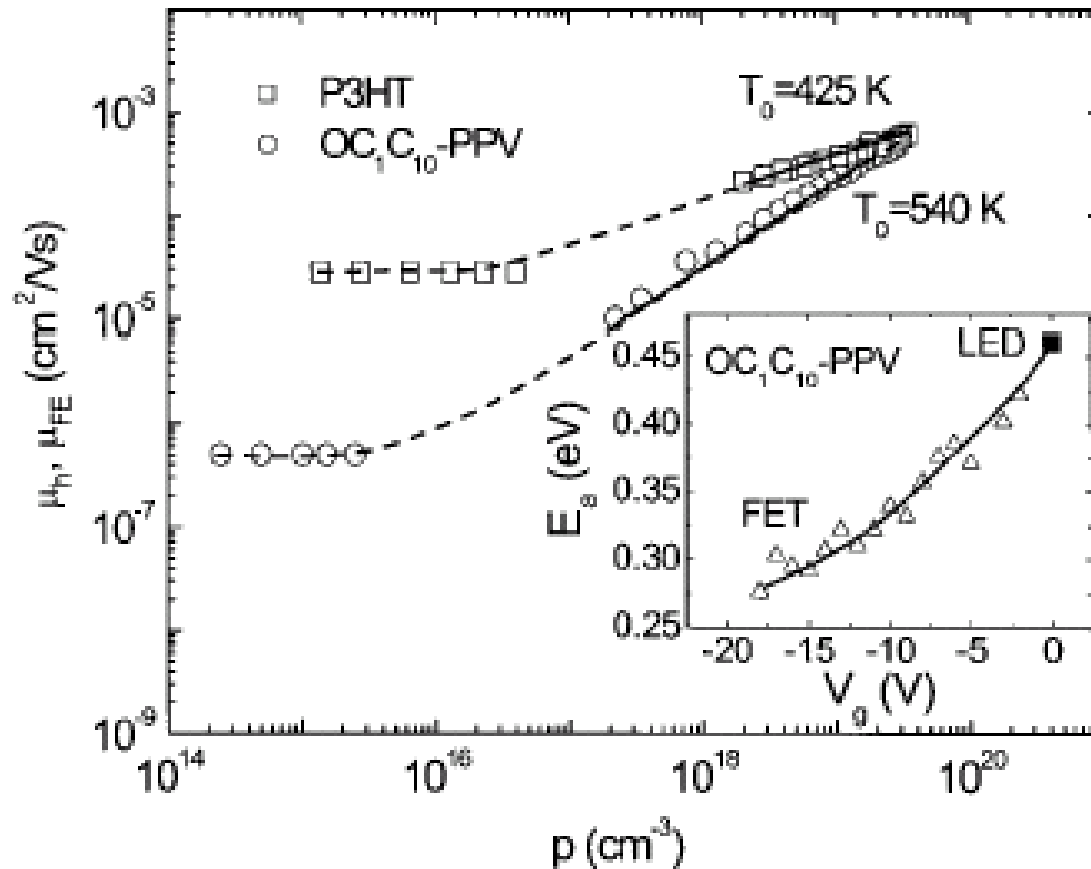
W.F. Pasveer, J. Cottaar, C. Tanase, R. Coehoorn, P.A. Bobbert, P.W.M. Blom, D.M. de Leeuw, and M.A.J. Michels, *Phys. Rev. Lett.* **94**, 206601 (2005).

Manifold filling



A. Troup *et al.*, *J. Non-Crystalline Solids* **35**, 151 (1980).

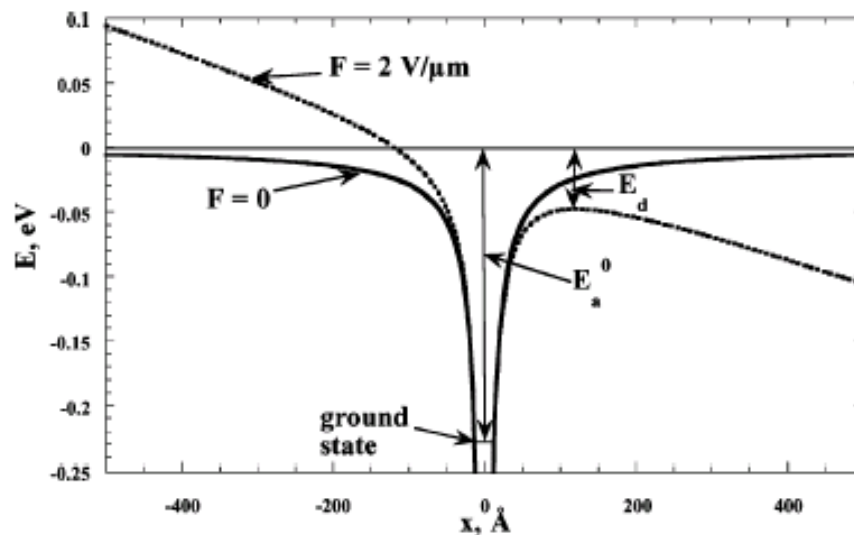
Mobility vs. charge density (II)



Charge density vs. electric field

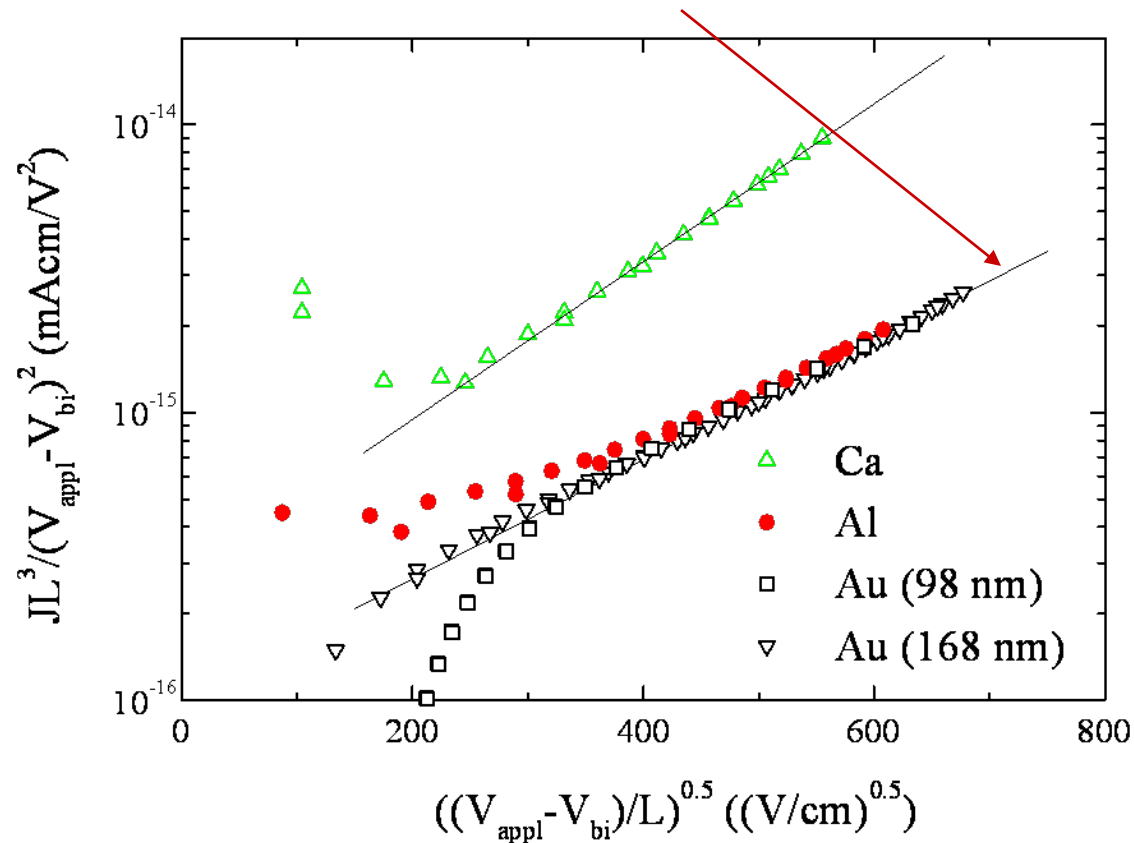
Field ionization of impurities leads to $n=n(E)$

$$J = q \mu_n F n_d \exp\left(\frac{\left(-E_a^0 + \left(\frac{q^3}{\pi \epsilon_0 \epsilon}\right)^{1/2} F^{1/2}\right)}{kT}\right)$$



Charge density vs. electric field (II)

$$J_{\text{SCL}} \approx (9/8) \epsilon \epsilon_0 \mu_0 V^2 \exp[0.89(V/E_0 L)^{0.5}] / L^3$$



Charge transport

First order correction:

Space charge effects

$$J = (9/8) \cdot \varepsilon \cdot \varepsilon_0 \cdot \mu \cdot V^2 / L^3$$



Disorder:

Energetics

Localized states



Influence on mobility

$$\mu = \mu(E, T)$$



Manifold filling:

Charge density dependence of mobility

$$\mu = \mu(n)$$



Charge generation:

Electric field dependence of charge density

$$n = n(E)$$



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Injection vs. transport

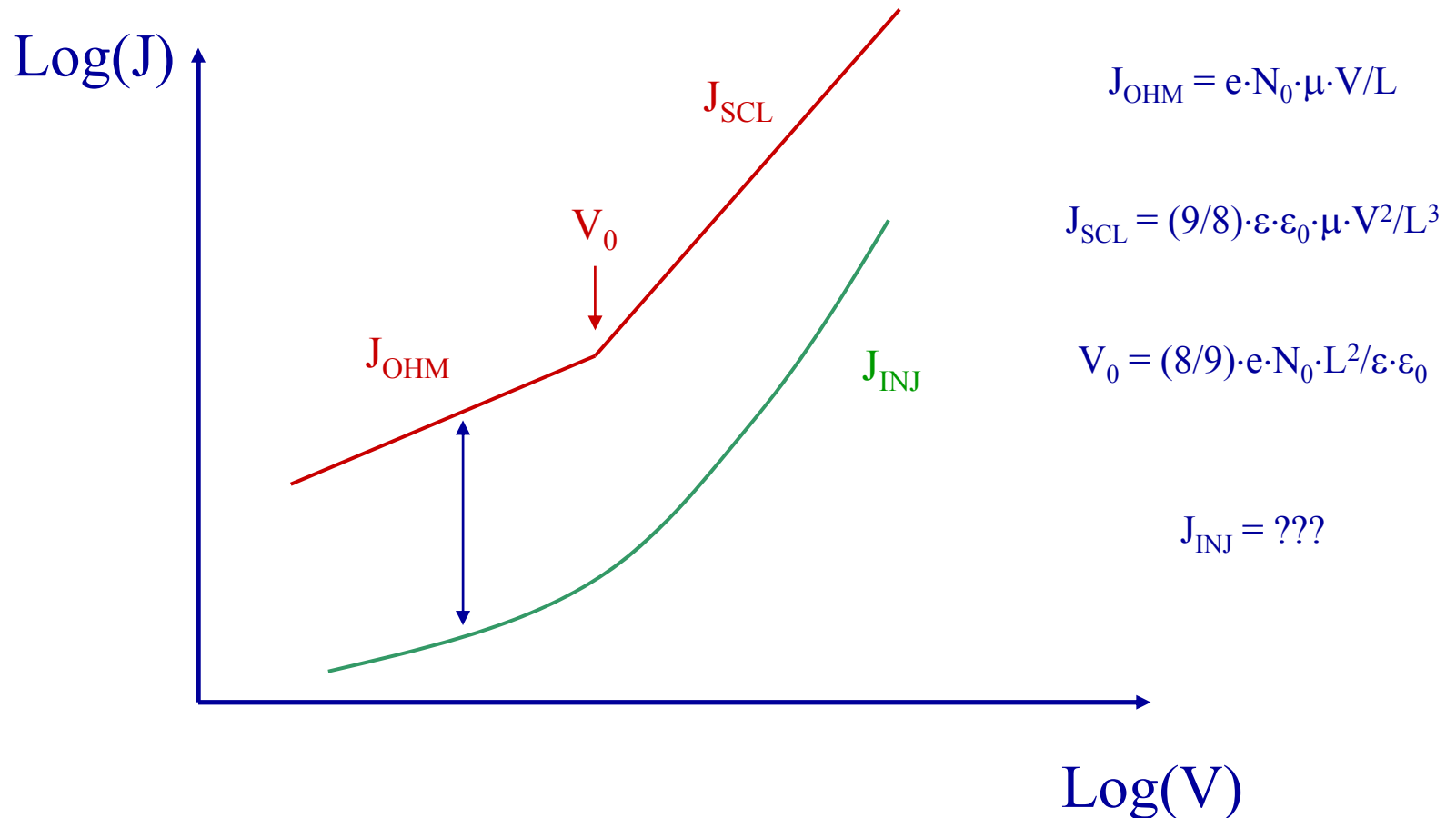


Figure of merit: $\eta = J_{\text{INJ}} / J_{\text{MAX}}$

Definition of an ohmic contact

A contact that satisfies the demands of the bulk for current.

$$\eta = 1$$

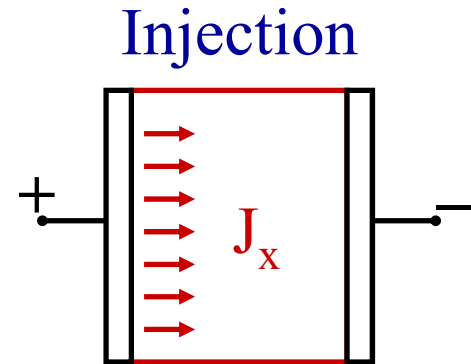
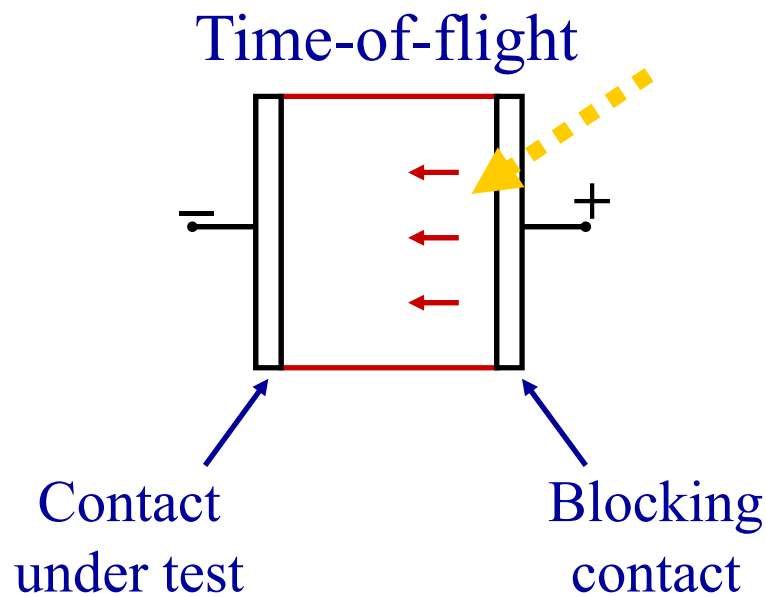
See: Y. Shen, A. Hosseini, M.H. Wong, and G.G. Malliaras, “How to make ohmic contacts to organic semiconductors”, *ChemPhysChem.* **5**, 16 (2004).



Cornell University

Separation of injection and transport (I)

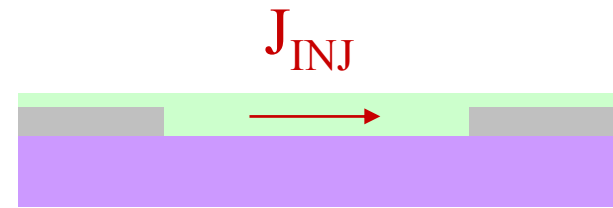
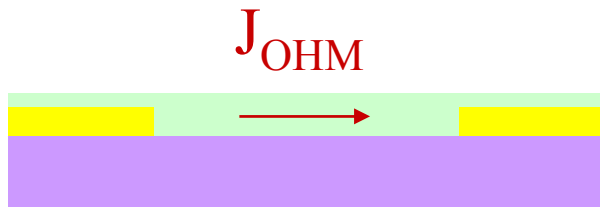
- Trap-free hole transporter
- Measure mobility \rightarrow Calculate $J_{SCL} (= (9/8) \cdot \epsilon \cdot \epsilon_0 \cdot \mu \cdot V^2 / L^3)$
- Measure injected current J_{INJ}



$$\eta = J_{INJ} / J_{SCL}$$

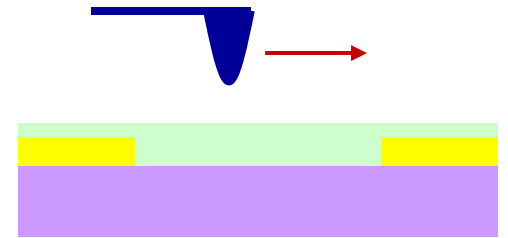
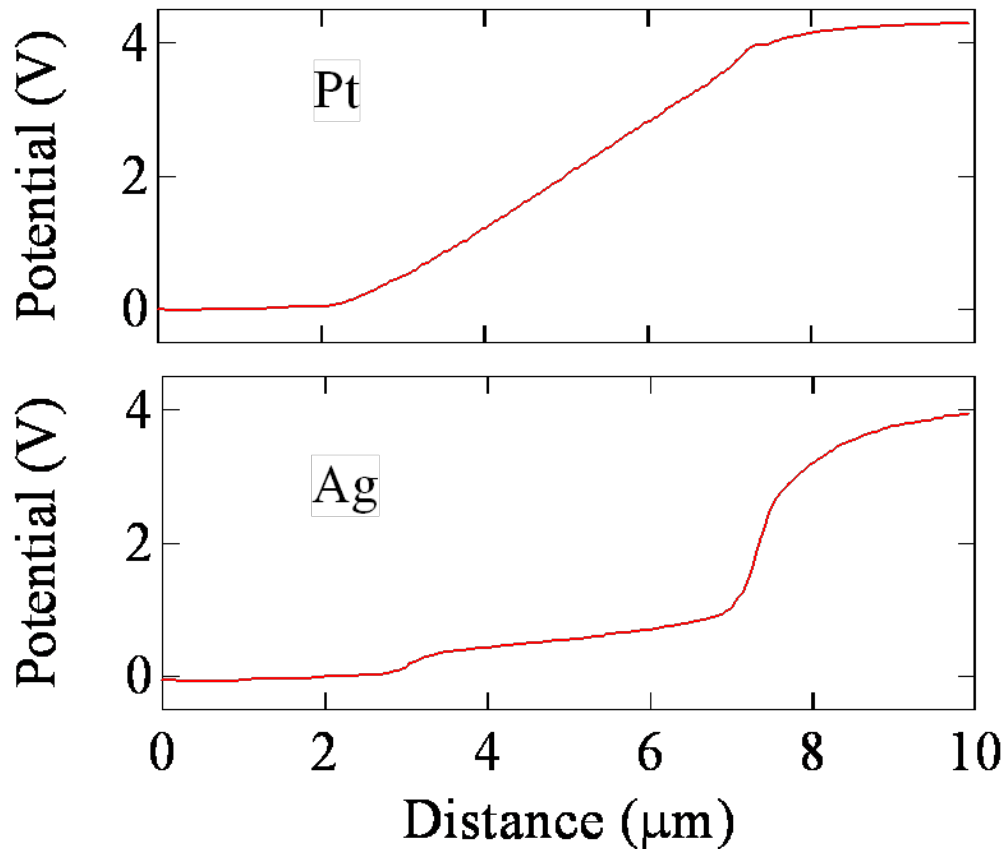
Separation of injection and transport (II)

- Measure J_{OHM} using Ohmic contact
- Compare with current from unknown contact



$$\eta = J_{\text{INJ}} / J_{\text{OHM}}$$

Separation of injection and transport (III)



Pt makes an ohmic contact to PC:TPD. Ag does not.

Hierarchy of injection models

Mechanism:

Thermionic emission

$$J = A \cdot \exp(-\phi/kT)$$

Tunneling

$$J = A \cdot E^2 \cdot \exp(-B \cdot \phi^{3/2}/E)$$

First order corrections:

Barrier lowering

$$J \sim \exp(E^{0.5})$$

Recombination with image force

$$J \sim \mu$$

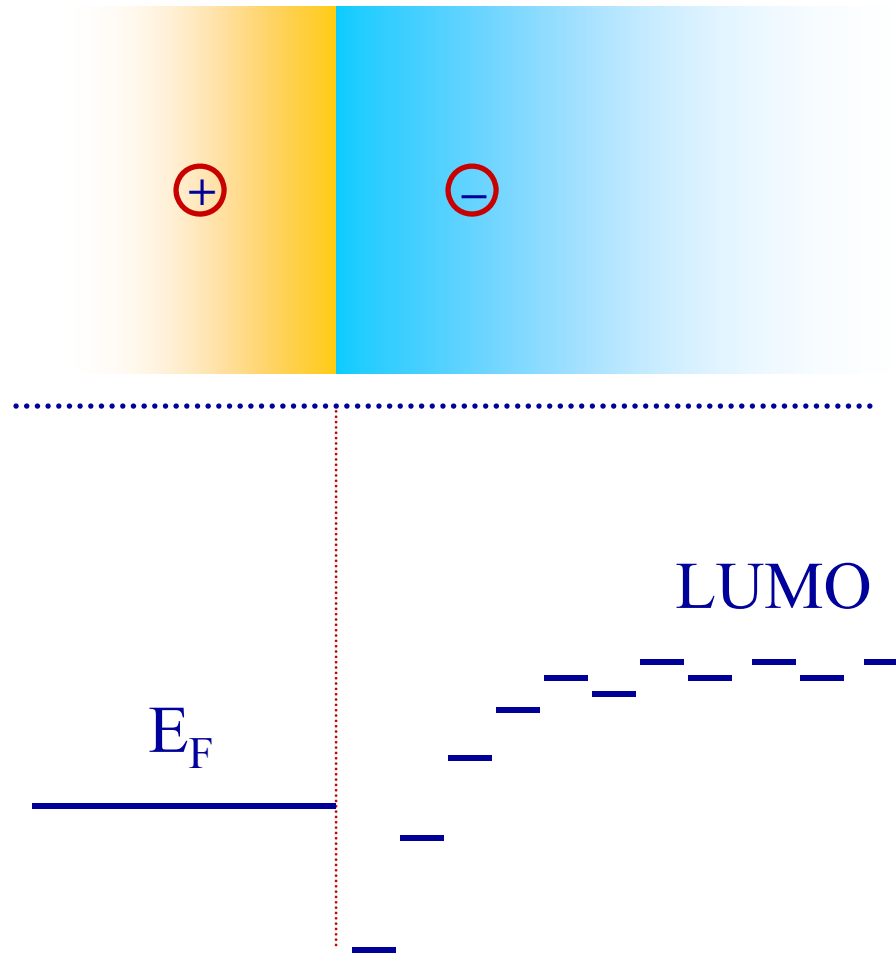
Disorder:

Gaussian disorder

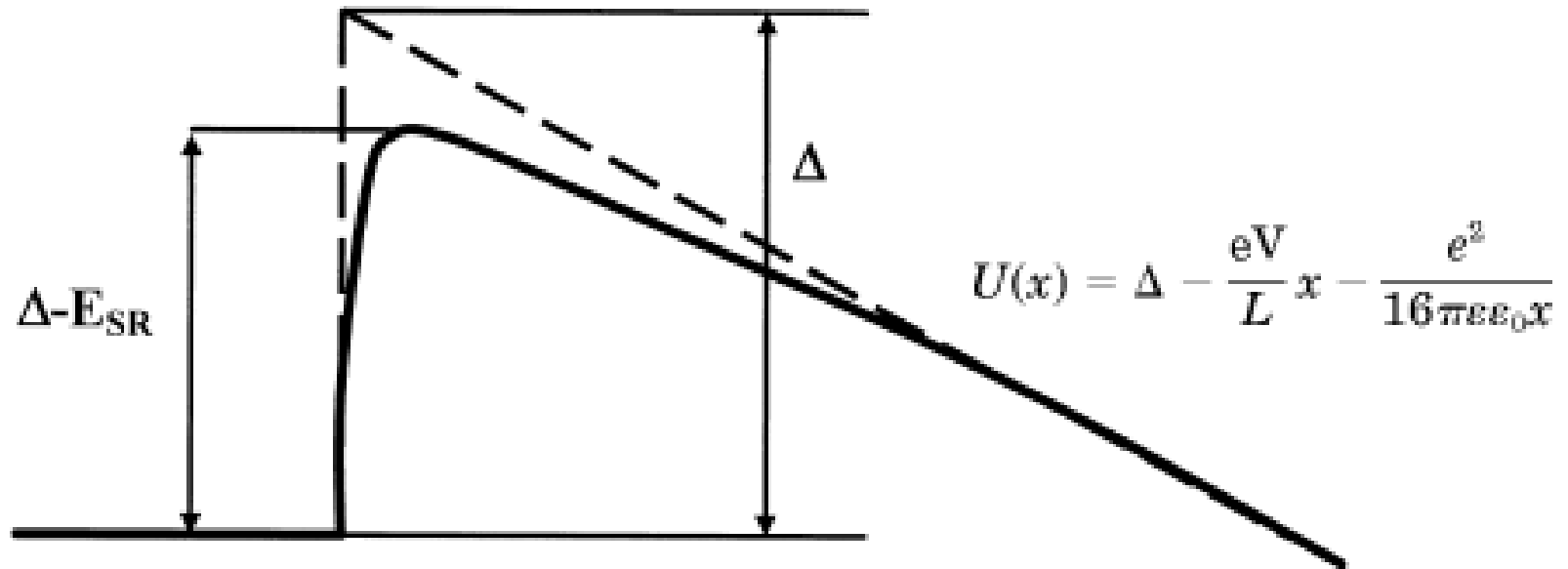
$$J \sim \exp(E^{0.5})$$



Image force



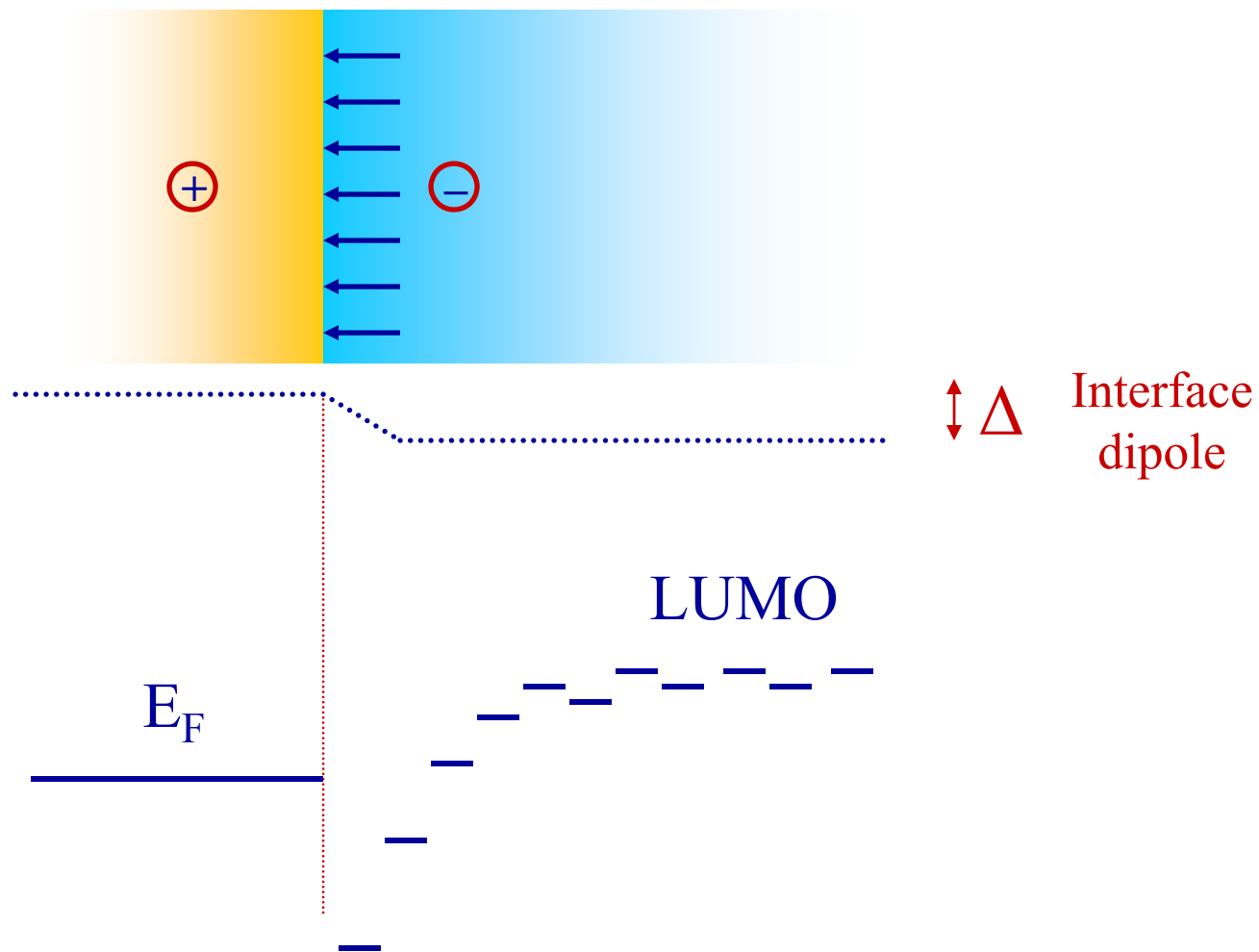
Barrier lowering



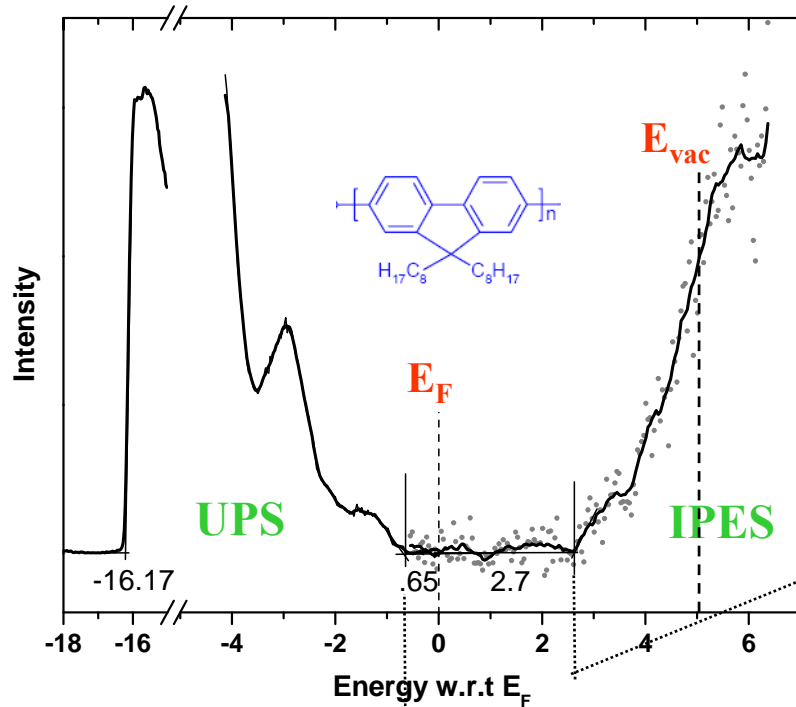
$$\Delta_{SR} = \Delta - E_{SR},$$

$$E_{SR} = \sqrt{\frac{V}{L} \frac{e^2}{4\pi\epsilon_0\epsilon}}$$

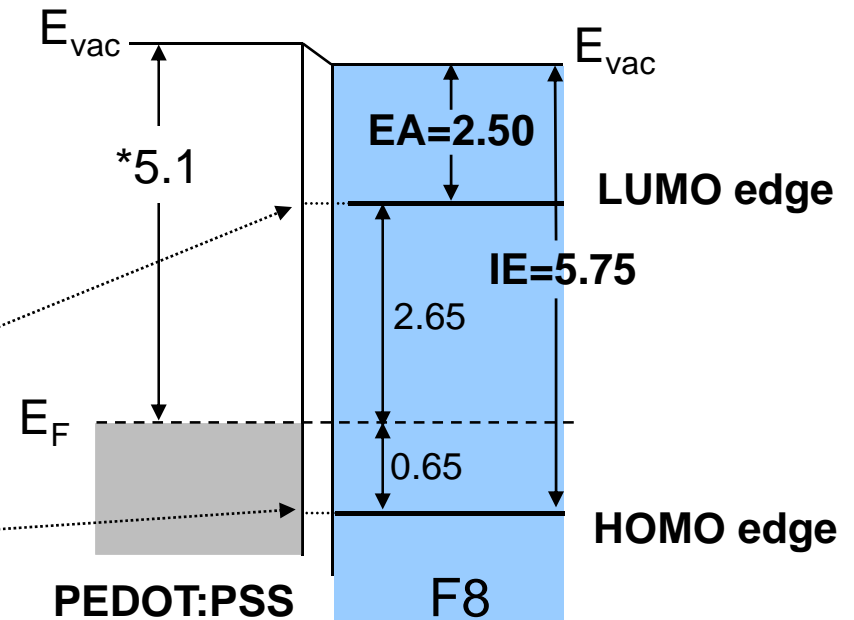
Interface dipole



Energetics at the contact



Ionization energy (IE) and electron affinity (EA) measured from HOMO and LUMO edges w.r.t vacuum level

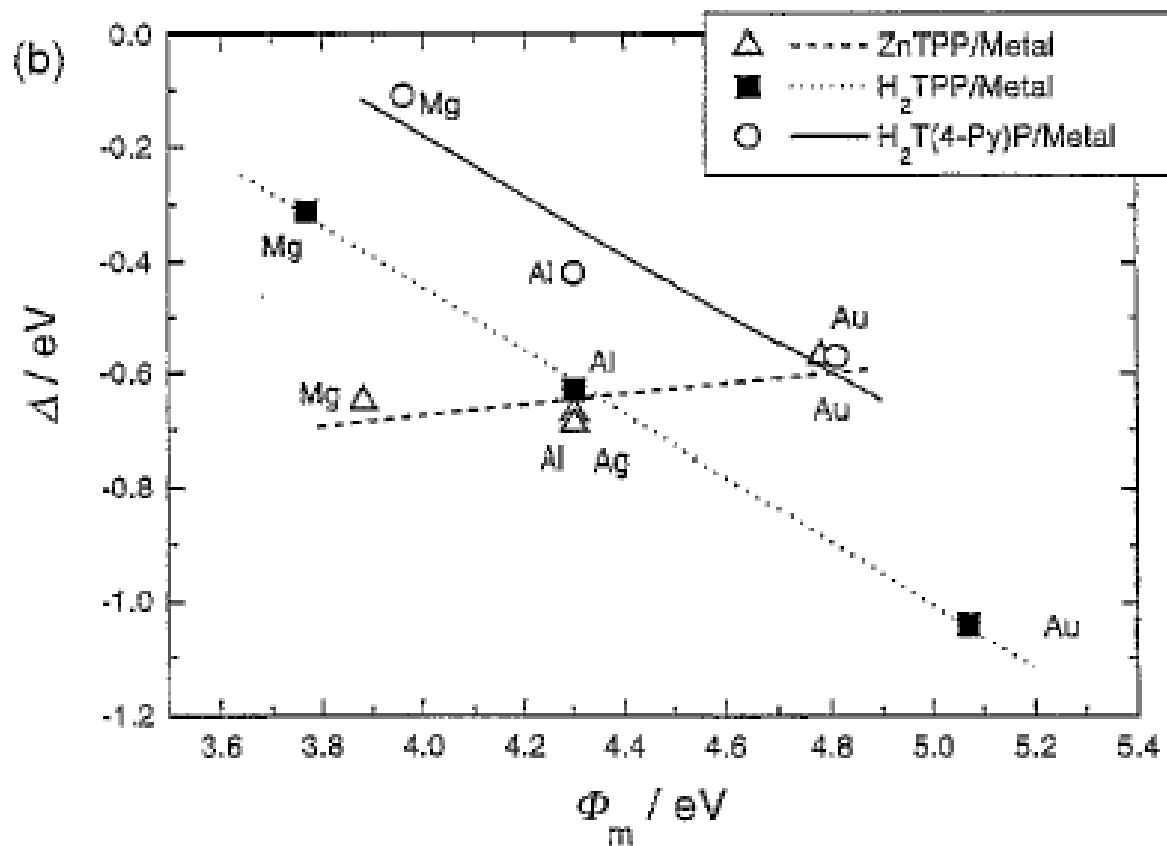


(energies in eV)

* Work function of PEDOT:PSS substrate measured on separate sample produced in same batch.

Kahn group - Princeton

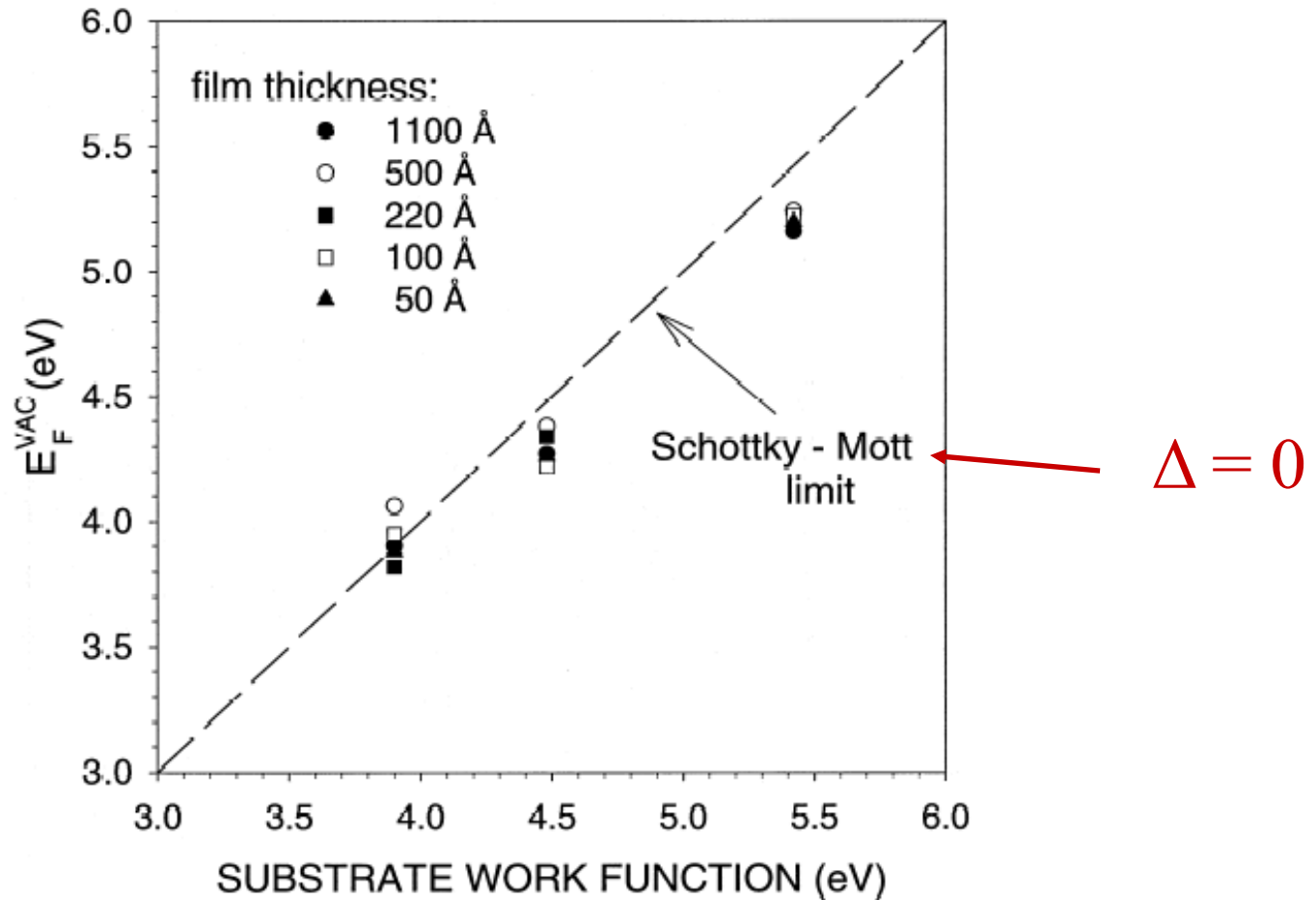
Magnitude of the dipole



K. Seki *et al.*, *Synth. Metals* **91**, 137 (1997).

Also: I.G. Hill *et al.*, *Appl. Phys. Lett.* **73**, 662 (1998).

Magnitude of the dipole (II)



Observation

“Surface science” vs. “realistic manufacturing conditions”:

Interfaces prepared under UHV show large dipoles

(*i.e.* barrier cannot be calculated if E_F , LUMO is known)

Interfaces prepared in ambient show negligible dipoles

(*i.e.* barrier scales with metal work function)

Influence on injection

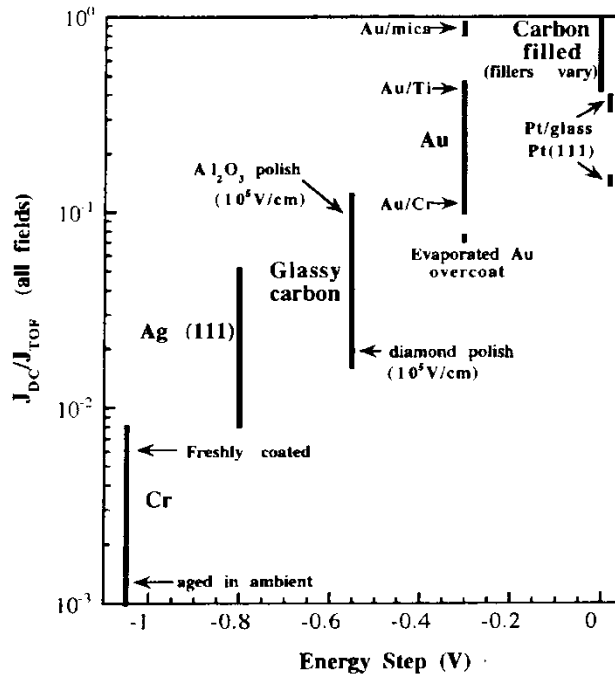
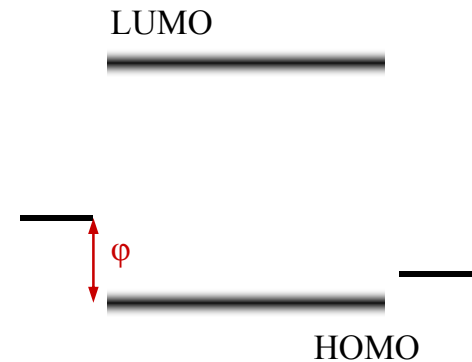


FIG. 6. Hole injection efficiency figure of merit for substrate contacts of varying work function vs. energy step across the contact polymer interface estimated from published work function data and electrochemical redox potential data. The height of each bar reflects the variability in injection efficiency due primarily to variation in substrate surface pretreatment and for the particular case of Au, diffusion to the interface of metal atoms from underlying binder layers.



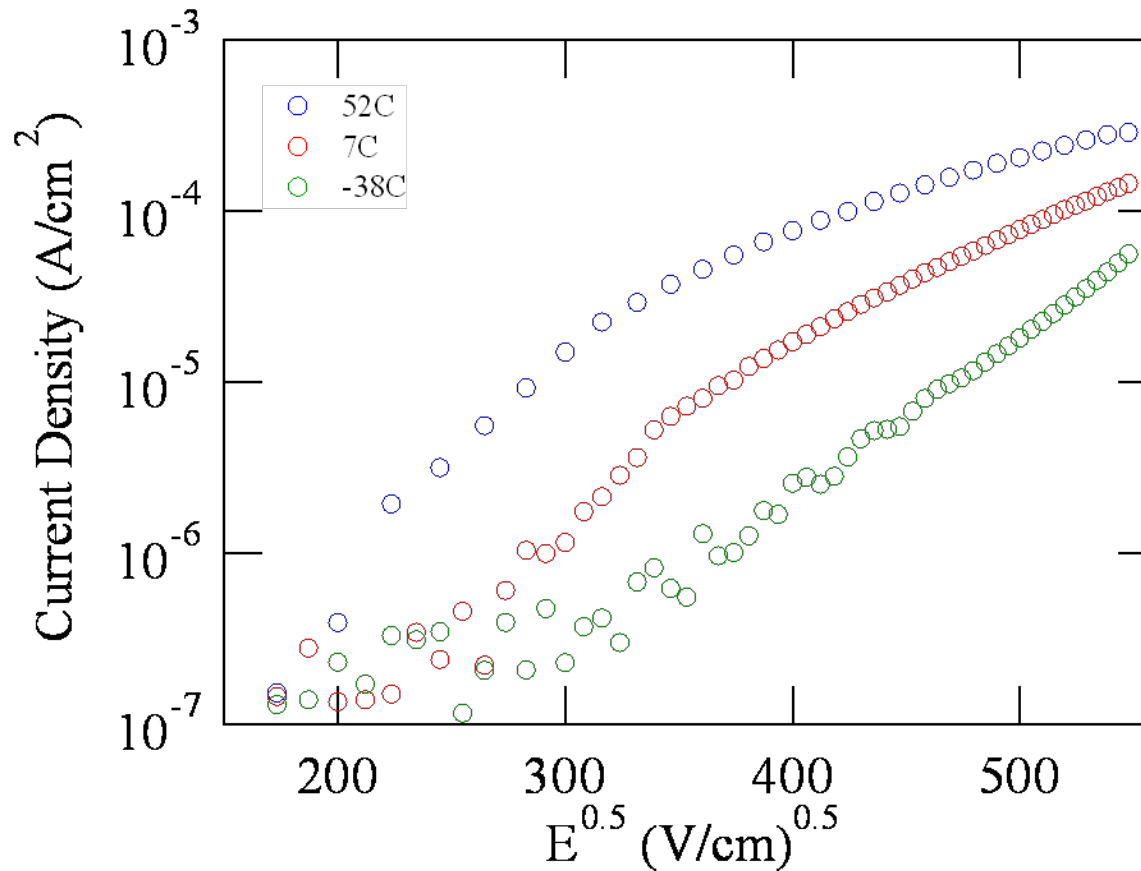
From:

M. Abkowitz *et al.*,

J. Appl. Phys. **83**, 2670 (1998).

Energetics dominates injection

Field dependence of injection



PEDOT:PSS/PFO

Injection in low mobility materials

RICHARDSON-SCHOTTKY EFFECT IN INSULATORS*

P. R. Emtage and J. J. O'Dwyer†

Westinghouse Research Laboratories, Pittsburgh, Pennsylvania

(Received 31 January 1966)

The Richardson-Schottky formula for thermionic emission from a metallic cathode into the conduction band of an insulator is frequently¹ stated as

$$J_S = \frac{4\pi em(kT)^2}{h^3} e^{-(\varphi_0 - \Delta\varphi)/kT}. \quad (1)$$

In this expression φ_0 is the work function, and the Schottky term is given by

$$\Delta\varphi = (e^3 F_c / \epsilon)^{1/2}, \quad (2)$$

where ϵ is the dielectric constant, and F_c the

field strength immediately in front of the cathode. It has recently been pointed out by Simmons² that this expression is invalid when the mobility of the electrons in the dielectric is low, for if one determines the density of current carriers in the insulator, n , from the relationship

$$J = ne\mu F, \quad (3)$$

one may then find that n becomes so large that back-diffusion from the dielectric to the metal will occur. Unfortunately Simmons's discus-

$$J = N \cdot e \cdot \mu \cdot E \cdot \exp(-\varphi_B/kT)$$

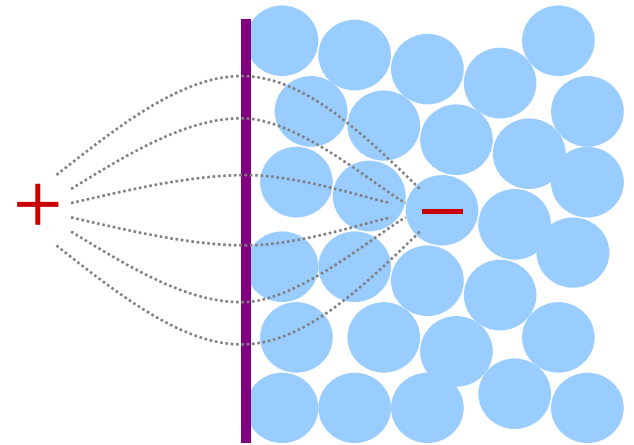
Recombination with image charge

$$J = C \exp(-\phi_B/kT) -en_0 S(E)$$

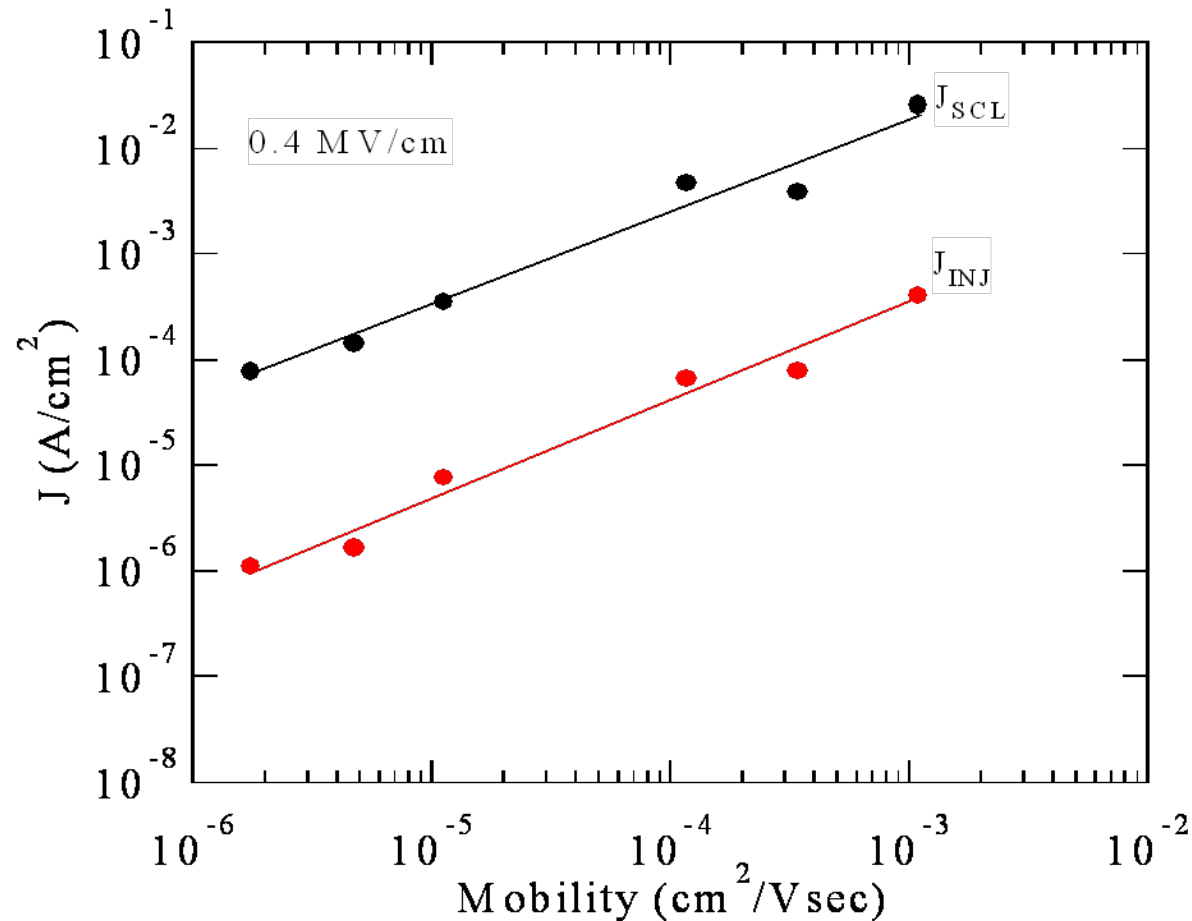
- Surface recombination as a hopping process in the image charge potential.
- No current flow at zero field.

$$C = 16\pi\epsilon\epsilon_0 N_0 (kT)^2 \mu / e^2$$

$$S(0) = 16\pi\epsilon\epsilon_0 (kT)^2 \mu / e^3$$

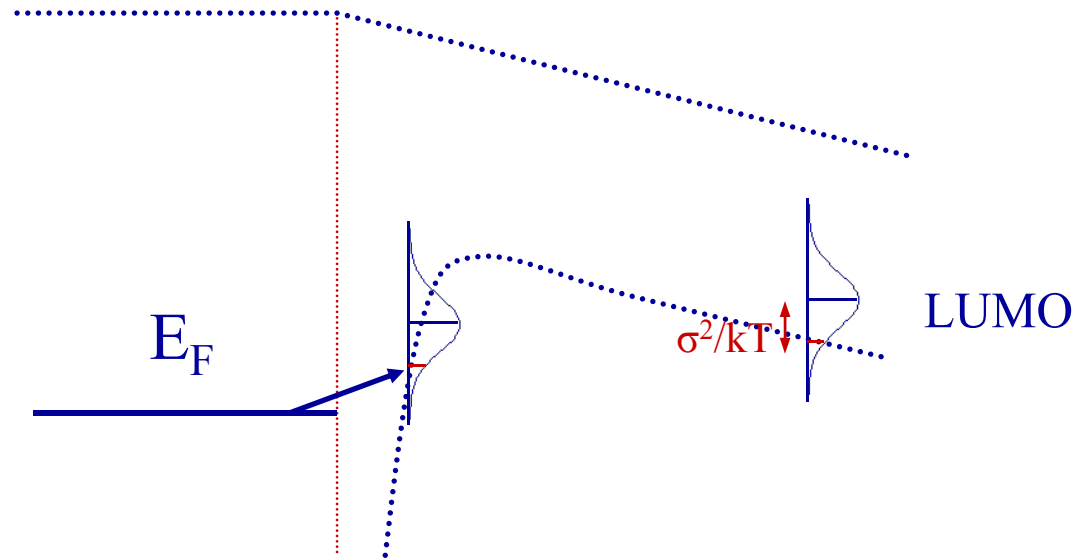


Dependence of injection on mobility



Y. Shen, M.W. Klein, D.B. Jacobs, J.C. Scott,
and G.G. Malliaras, *Phys. Rev. Lett.* **86**, 3867 (2001).

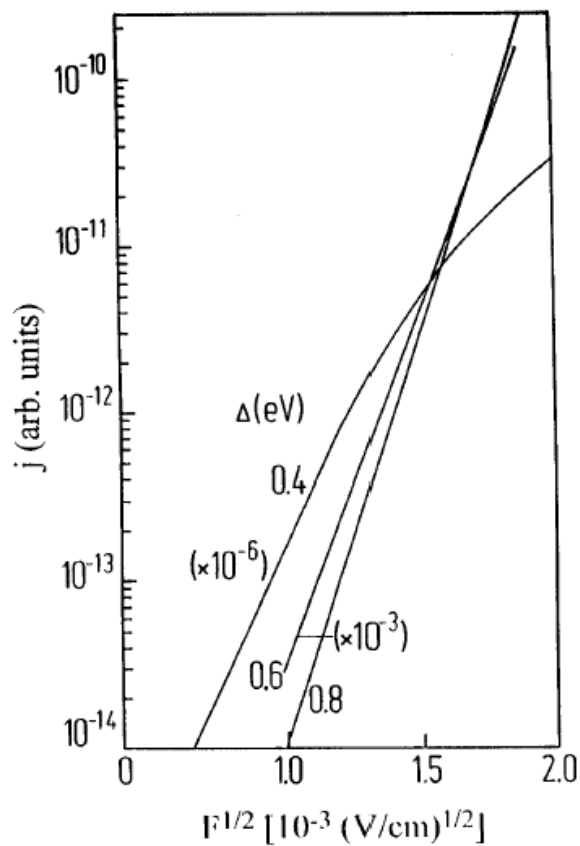
Gaussian disorder



$$J_{Inj} = e \cdot \nu \cdot \int_a^{\infty} dx_0 \left[\exp(-2 \cdot \gamma \cdot x_0) \cdot w_{esp}(x_0) \right] \cdot \int_{-\infty}^{\infty} dE [Bol(E) \cdot g(U(x_0) - E)]$$

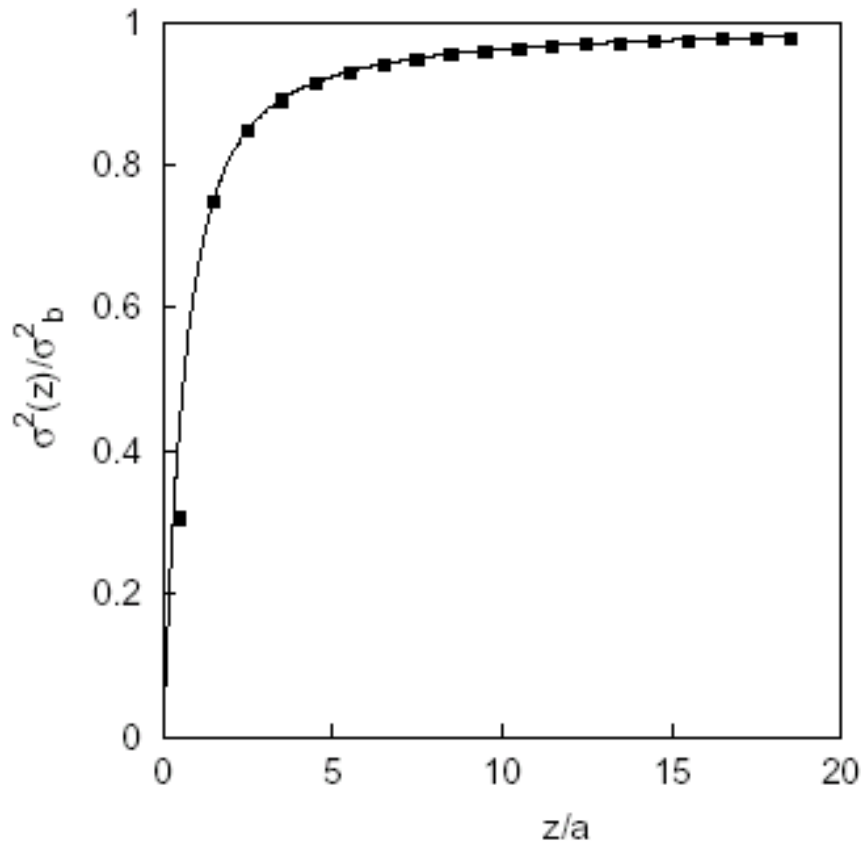
First hop is the rate limiting step

Gaussian disorder (II)



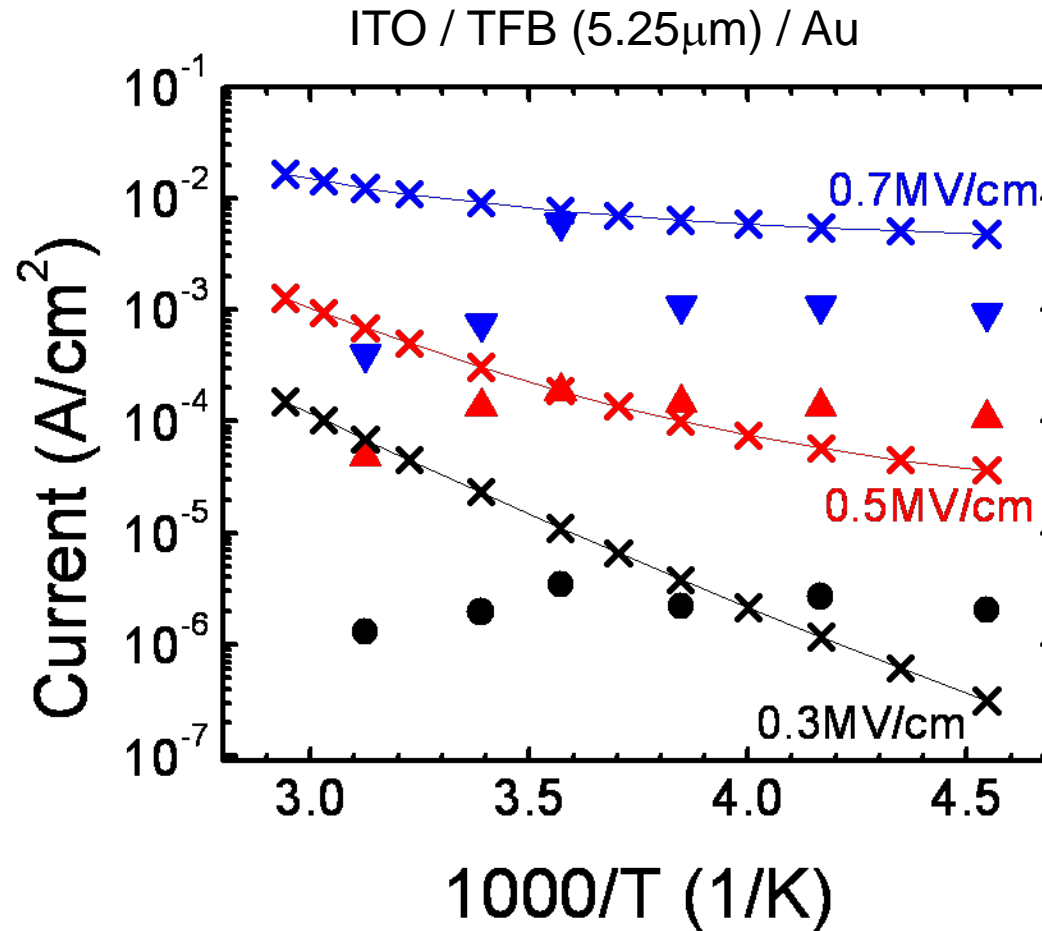
Field
dependence
resembles
thermionic
emission

Gaussian disorder (III)

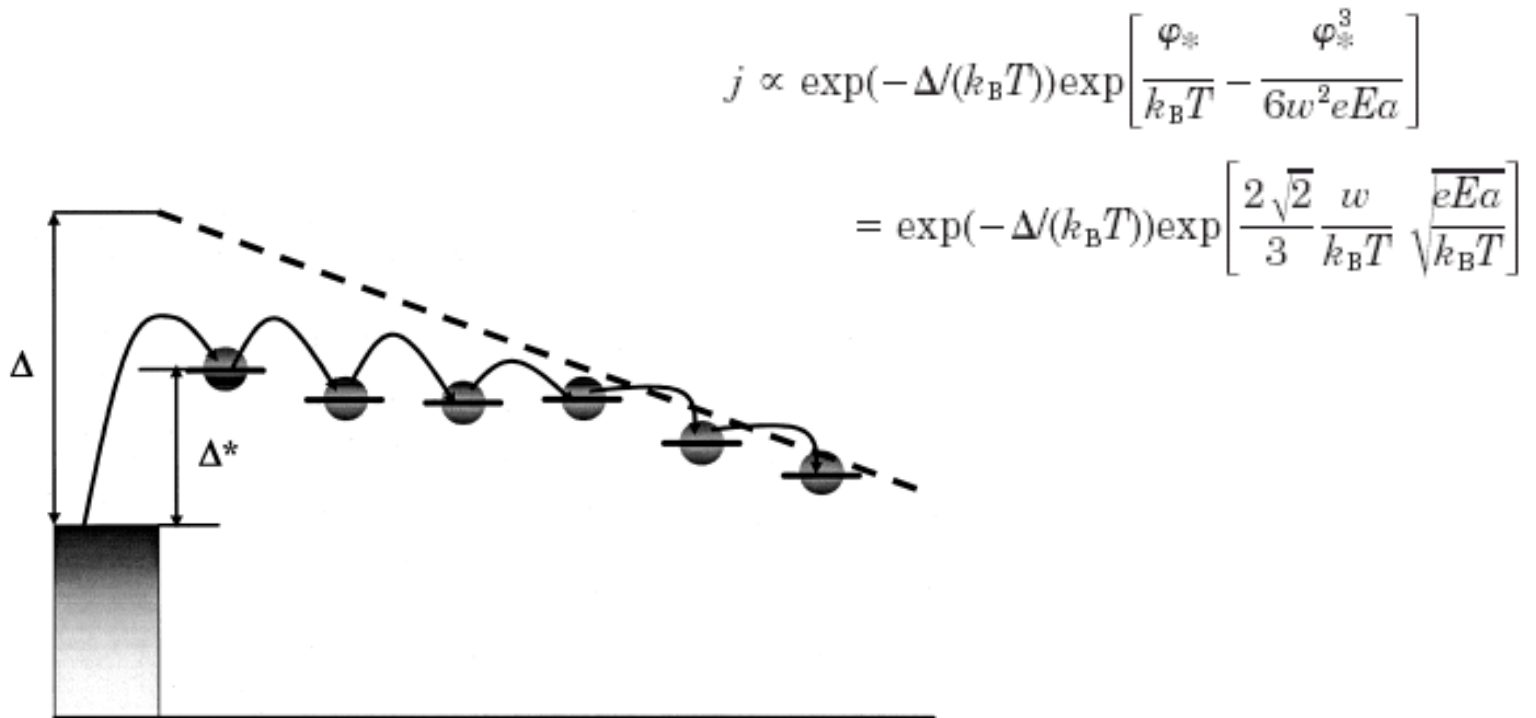


Energetic
disorder due to
charge-dipole
interactions
different at the
interface

Fit to the data



Preferential pathways model



$$j \propto \exp(-\Delta/(k_B T)) \exp\left[\frac{\varphi_*}{k_B T} - \frac{\varphi_*^3}{6w^2 e E a}\right]$$

$$= \exp(-\Delta/(k_B T)) \exp\left[\frac{2\sqrt{2}}{3} \frac{w}{k_B T} \sqrt{\frac{e E a}{k_B T}}\right]$$

Charge injection

Mechanism:

Thermionic emission

$$J = A \cdot \exp(-\phi/kT)$$

Tunneling

$$J = A \cdot E^2 \cdot \exp(-B \cdot \phi^{3/2}/E)$$

First order corrections:

Barrier lowering

$$J \sim \exp(E^{0.5})$$



Recombination with image force

$$J \sim \mu$$



Disorder:

Gaussian disorder

$$J \sim \exp(E^{0.5})$$



Opportunities

- There is rich physics to be explored in organic devices
- Organic materials that show ideal transport characteristics and high mobilities have become available
- Charge injection in is often poor (and poorly understood) – opportunity for major improvements in organic device performance

Challenges

- Picture of metal/organic interfaces from spectroscopy is only now getting incorporated in injection models
- Injection expected to be spatially inhomogeneous due to correlated disorder
- $J \sim \exp(E^{0.5})$ ubiquitous, temperature range rather small
– need other tests for theories