
Modelling the Organic Solar Cell

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11th December, 2008

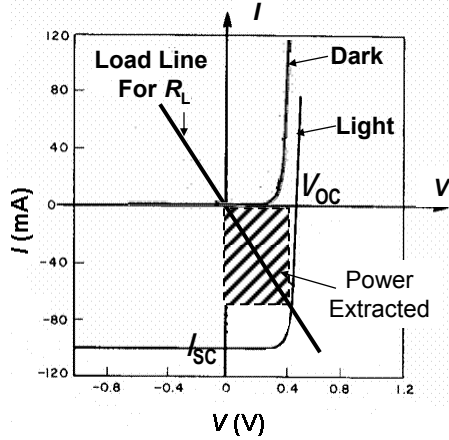
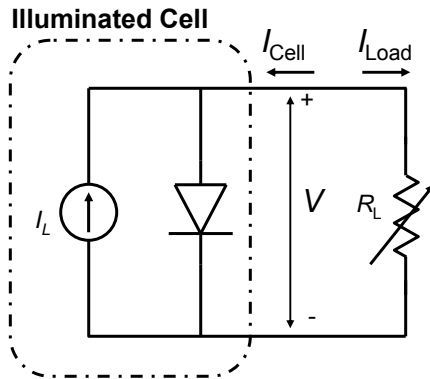
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Outline

- A brief review
- Short Circuit Current
 - Quantum Efficiency
- Open Circuit Voltage
- Fill Factor

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Power Extracted Out Of Solar Cell



□ $I_{Cell} = I_s [\exp(qVI/nkT) - 1] - I_L$; and $I_{Load} = VR_L$

□ Choose R_L to get maximum power

S.M.Sze 1991

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Factors Affecting Efficiency

□ I_{sc} (J_{sc}) – Short Circuit Current (density)

□ V_{oc} – Open Circuit Voltage

□ FF – Fill Factor

□ Maximum Power Output

$$P_{max} = V_{oc} \times I_{sc} \times FF$$

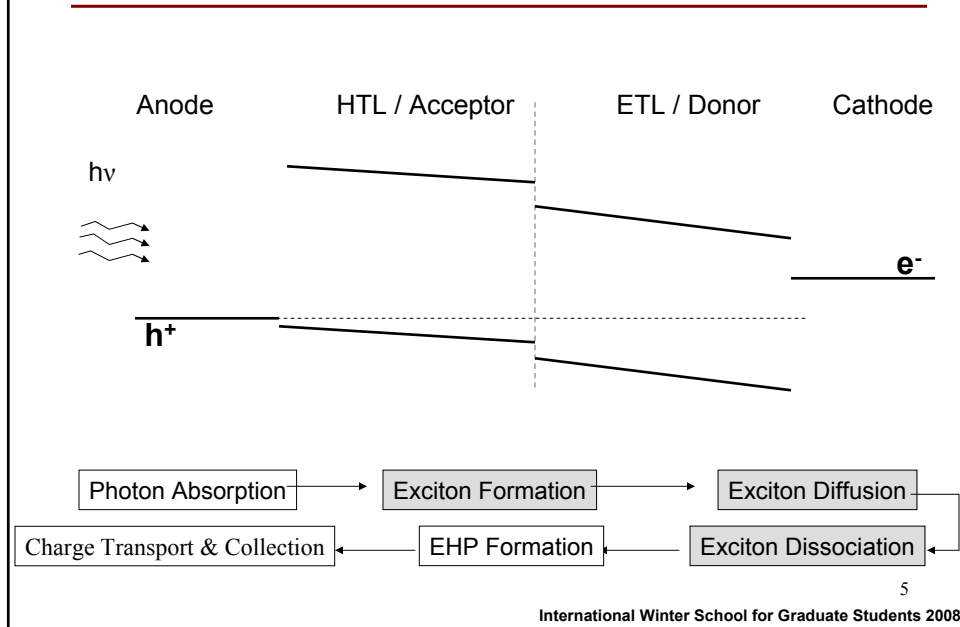
□ Efficiency

$$\eta = P_{max} \div \text{Incident Light Power}$$

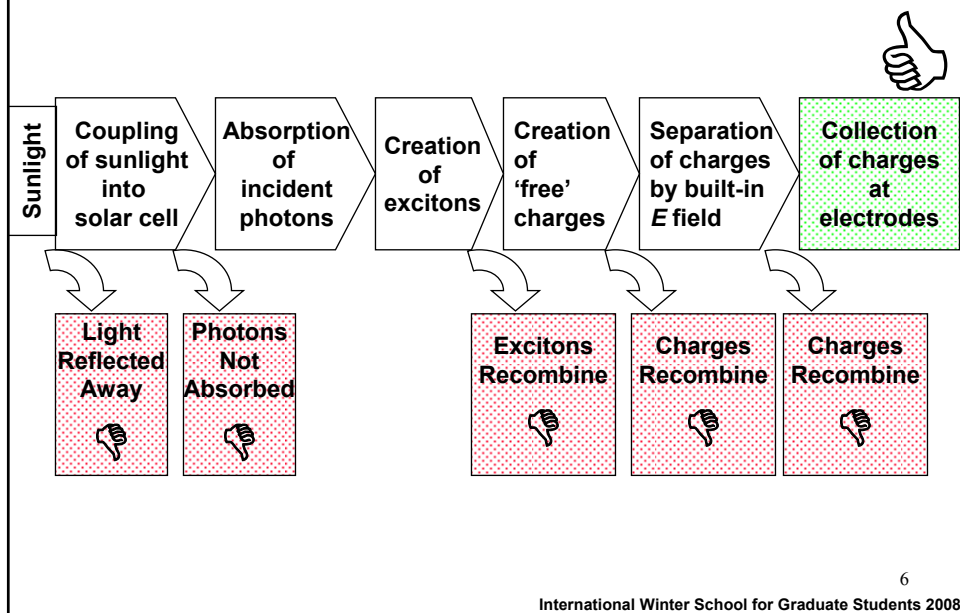
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Operation of Organic Solar Cells



Photovoltaic Process In Organic Solar Cells

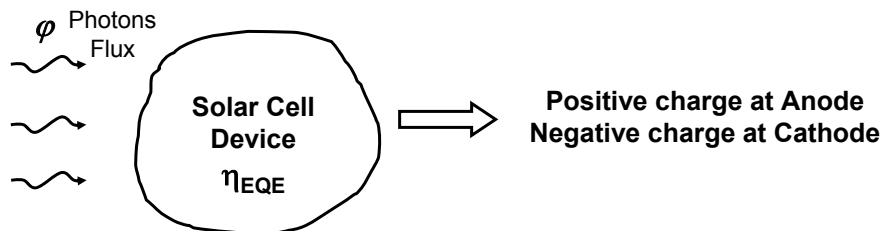


I_{sc} : Short Circuit Current

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Short Circuit Current & Quantum Efficiency



$$I_{sc} = \phi \eta_{EQE} q A$$

I_{sc} : Short Circuit Current when electrodes are shorted (A)

ϕ : Photon flux (# of photons $s^{-1} m^{-2}$)

A : Area of device

η_{EQE} : External Quantum Efficiency = $\eta_0 \cdot \eta_A \cdot \eta_{ED} \cdot \eta_{CT} \cdot \eta_{CC}$

q : Electron charge (C)

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Quantum Efficiency

$$\begin{aligned}\eta_{EQE} &= \eta_O \cdot \eta_A \cdot \eta_{ED} \cdot \eta_{CT} \cdot \eta_{CC} \\ &= \eta_O \cdot \eta_{IQE}\end{aligned}$$

η_{EQE} : External Quantum Efficiency

η_{IQE} : Internal Quantum Efficiency

η_O : Optical efficiency

η_A : Light Absorption Efficiency

η_{ED} : Excitation Diffusion Efficiency

η_{CT} : Charge Transfer Efficiency

η_{CC} : Charge Collection Efficiency

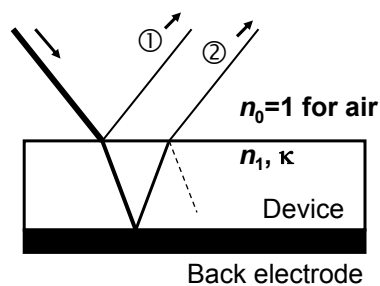
η_{EQE} is the percentage of incident photons that result in carries contributing to short circuit current

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Optical Efficiency η_o

η_o



□ Optical losses maybe due to

- Reflection at the surface ①
- Unabsorbed light leaking out ②

□ Solutions

- Anti Reflection Coating (ARC)
- Texturing the top surface
- Concentrators

$\eta_o = 1 - R$ where

$$R = \frac{(n_1 - n_0)^2 + \kappa^2}{(n_1 + n_0)^2 + \kappa^2}$$

n_i : refractive index of medium i

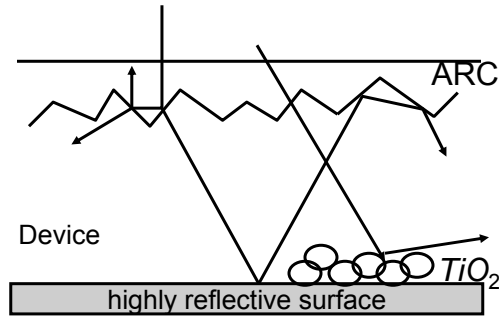
κ : attenuation coefficient in device

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Light Trapping

η_o



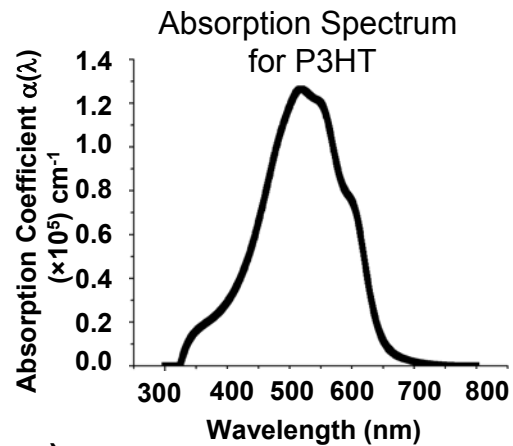
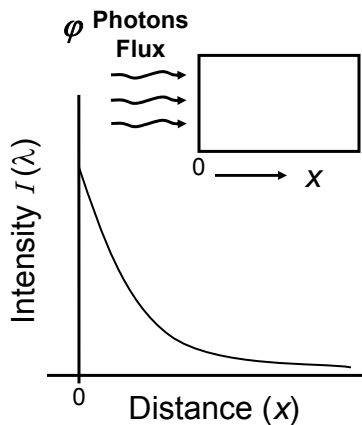
- Surface modification
- Anti-reflection coating
- Nanoparticles such as TiO_2

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Light Absorption

η_A



$$I(\lambda, x) = I(\lambda, x = 0) \exp(-\alpha x)$$

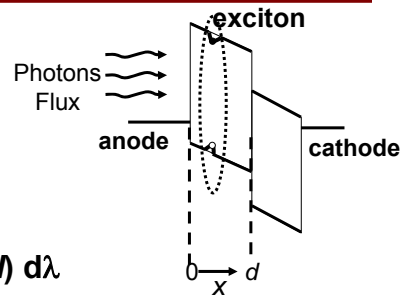
$$\phi = I(\lambda, x) / (h\nu/\lambda) \quad \begin{array}{l} h : \text{Plank's constant} \\ c : \text{Speed of light} \end{array}$$

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Absorption Efficiency η_A

η_A



$$\eta_A = 1 - \frac{\int_{\text{Full spectrum}} (hv/\lambda)^{-1} I(\lambda) \exp(-\alpha(\lambda)d) d\lambda}{\int_{\text{Full spectrum}} (hv/\lambda)^{-1} I(\lambda) d\lambda}$$

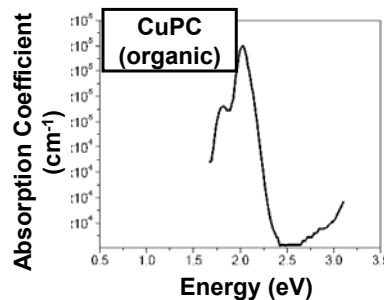
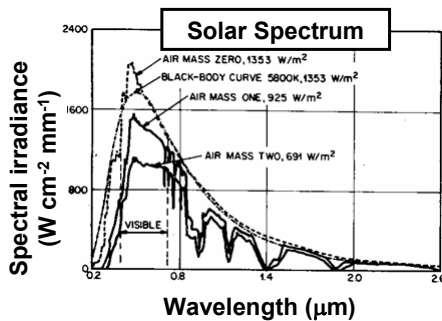
$$= \frac{\text{Number of photons absorbed}}{\text{Number of photons incident}}$$

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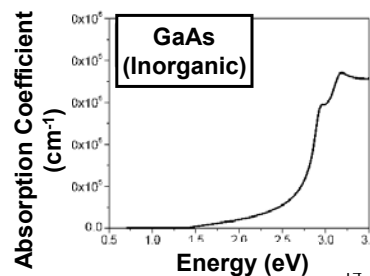
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Absorption in Active Layer

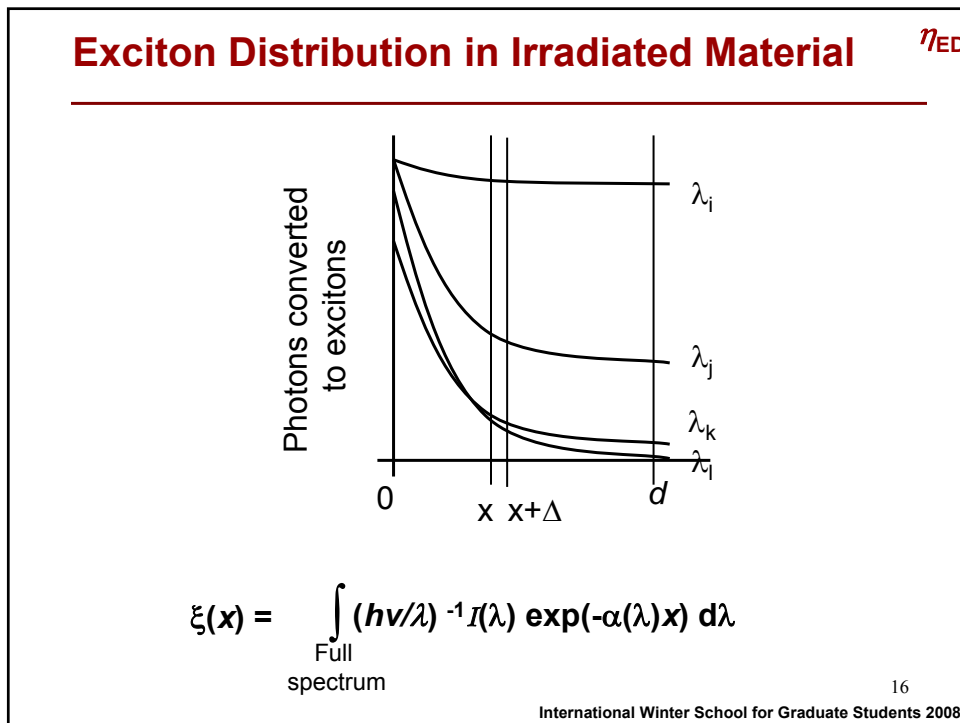
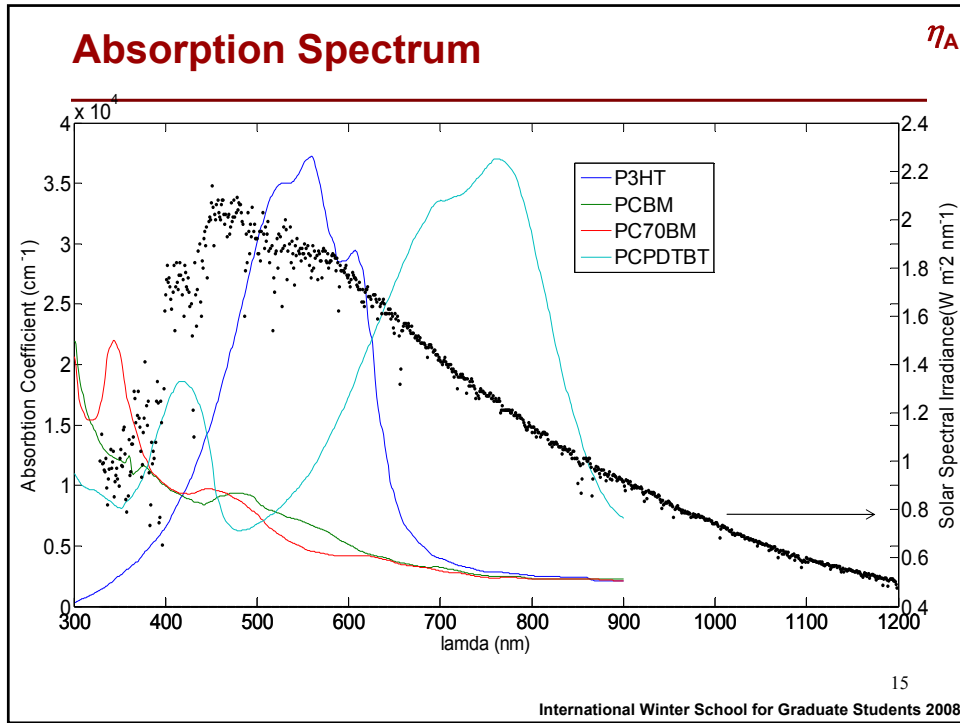
η_A



- Organics absorb in a band
- High absorption coefficient
- η_A is high for thick films



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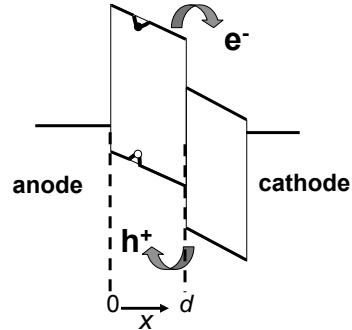
Exciton Dissociation Efficiency - η_{ED}

η_{ED}

- ❑ Excitons are neutral
- ❑ Concentration of surviving excitons at x' is

$$\xi(x+x') = \frac{1}{2} \xi(x) \exp(-x'/L_D)$$

- L_D is the average exciton diffusion length
- ❑ Likely location of dissociation is the interface



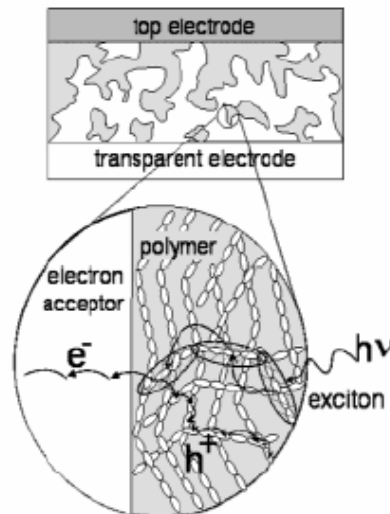
$$\eta_{ED} = \frac{\int_0^d \frac{1}{2} \xi(x) \exp(-(d-x)/L_D) dx}{\int_0^d \xi(x) dx} = \frac{\text{Excitons reaching interface}}{\text{Number of excitons created}}$$

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η_{ED} in Bulk Heterojunction Device

η_{ED}



$$\eta_{ED} \approx 1$$

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Charge Transfer Efficiency - η_{CT}

η_{CT}

- Electrons and hole drift towards electrodes
- On the way, they may get trapped/recombine
- Concentration of surviving charge will be

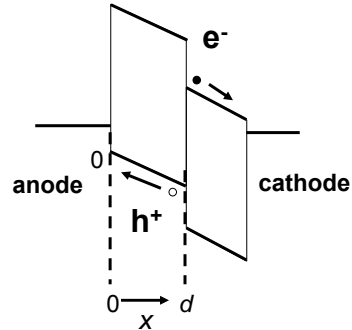
$$n(t) = n(t=t_0) \exp(-t/\tau)$$

- τ is the average charge lifetime

- Time needed for charge to reach the electrode

$$T_{\text{transit}} = d / [\mu(\mathcal{E}) \mathcal{E}]$$

- $\eta_{CT} = \exp(-T_{\text{transit}}/\tau) = \frac{\text{\# charges reaching electrode}}{\text{\# conducting charges created}}$



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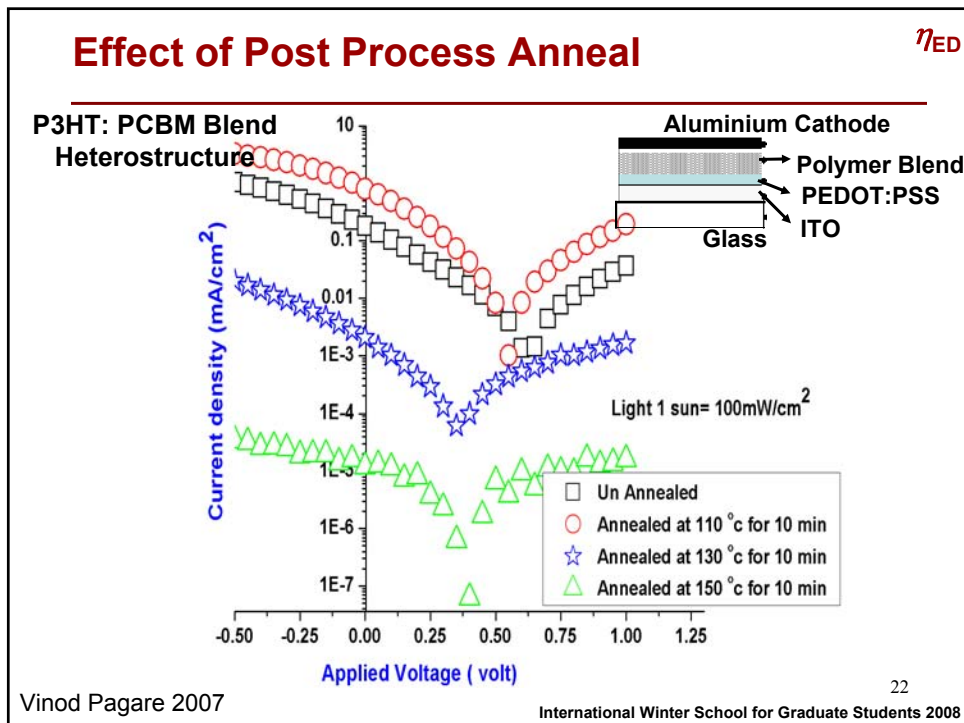
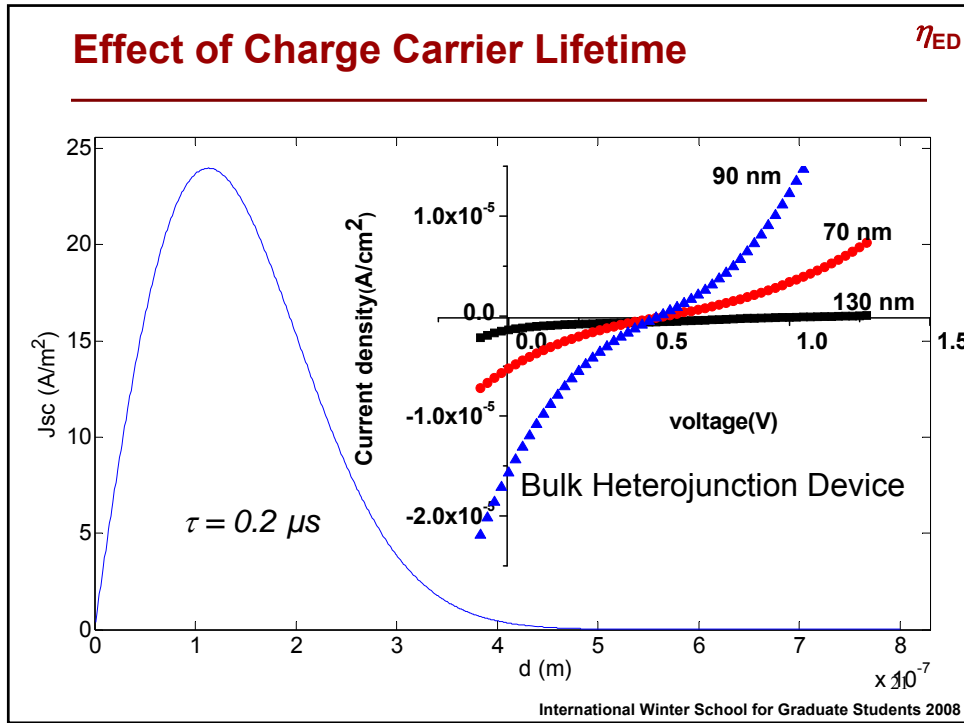
Factors Affecting η_{ED}

η_{ED}

- Choice of Electrodes
- Thickness of active layer(s)
- Morphology and Phase in active layer

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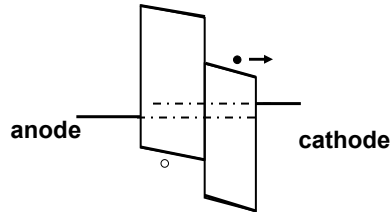
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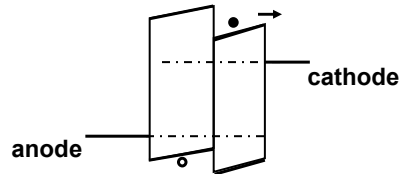
Charge Collection Efficiency - η_{CC}

η_{CC}

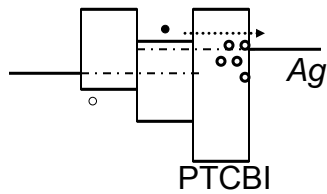
At low biases



At higher biases ($> V_{FB}$)



Tunnel through EBL



Charge collection may be affected by

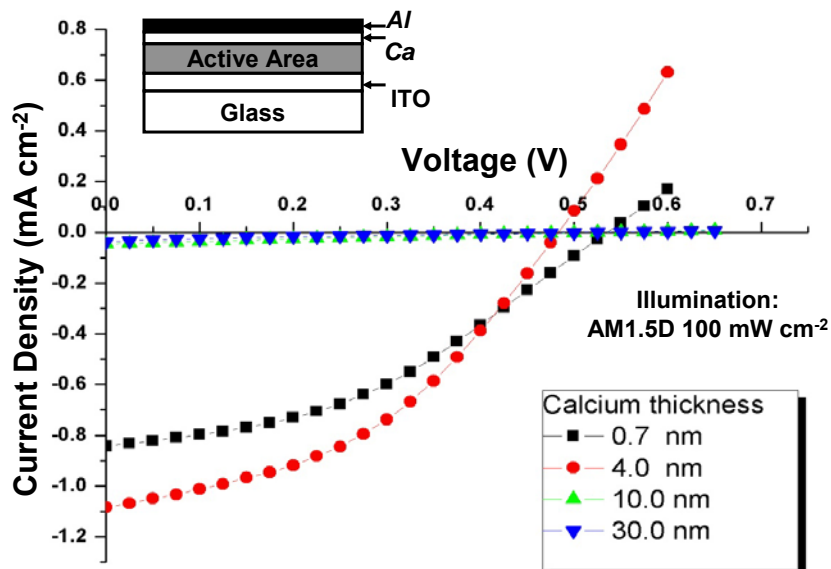
- Internal fields
- Traps
- Exciton Blocking Layer (EBL)

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Cathode Thickness Variation

η_{CC}



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Nitin Sahai 2008

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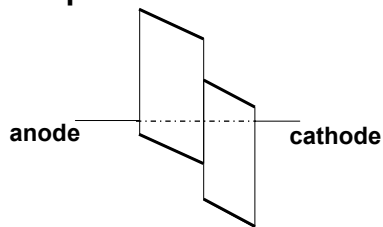
V_{oc} : Open Circuit Voltage

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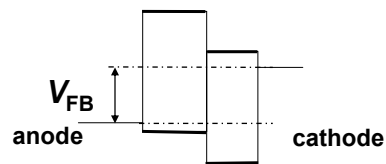
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Maximum Open Circuit Voltage

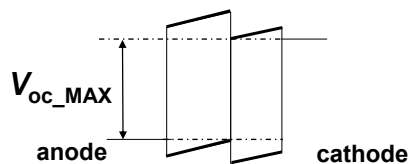
Equilibrium Condition



Flat Band Condition



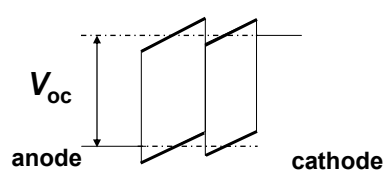
Max V_{oc} Bias Condition



$$V_{oc_MAX} = \phi_{LUMO_A} - \phi_{HOMO_D};$$

$$V_{oc} = \phi_{LUMO_A} - \phi_{HOMO_D} - 2kT \ln(g_D/p_D)$$

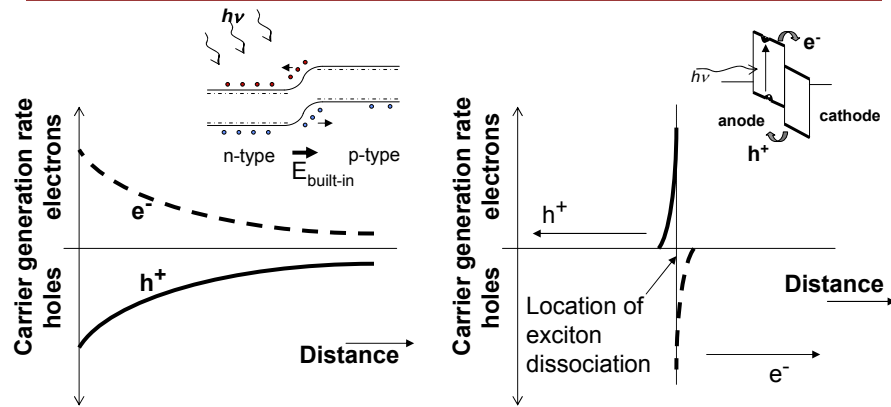
Thermodynamically Unstable



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Higher V_{oc} in Organic Solar Cells



Inorganic p-n junction Solar Cell

- Charge separation field has to overcome diffusion tendency of electron or hole to separate the charges

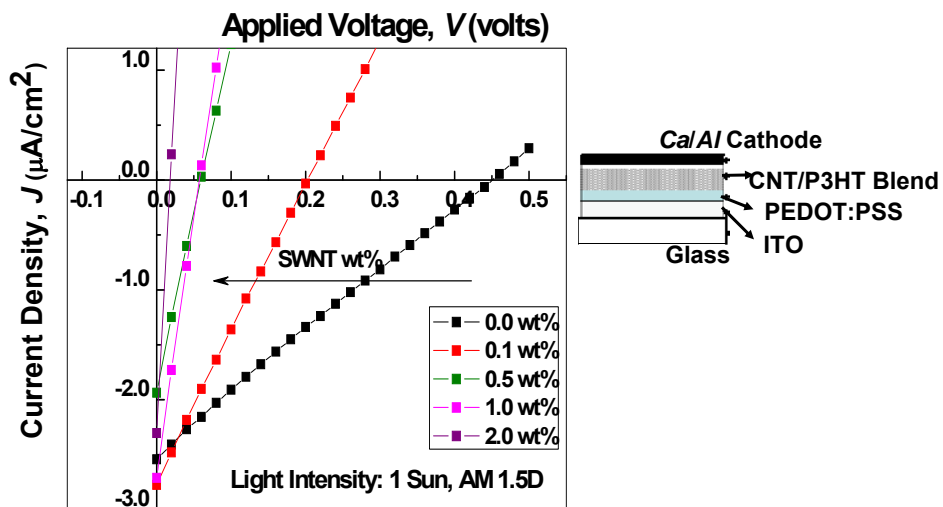
Organic hetero-junction Solar Cell

- Charge separation field is aided by the diffusion tendency of hole and electron

B. Greg 2003

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Lower R_{sh} Lowers V_{oc}

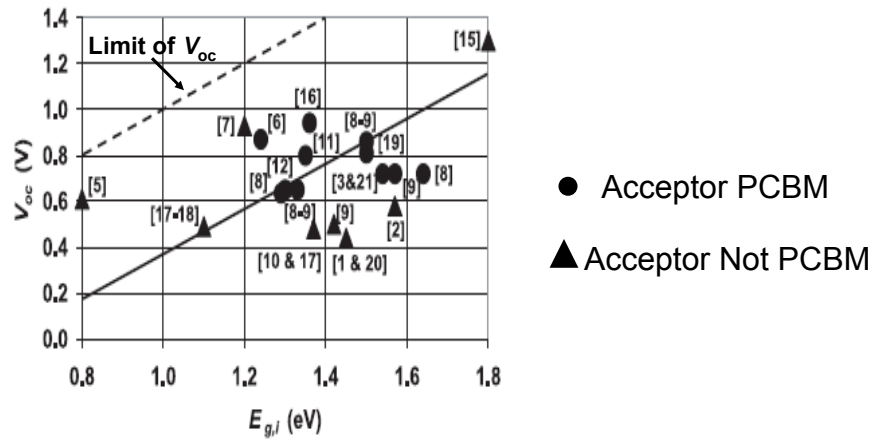


Arun Tej Mallajosyula 2008

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V_{oc} in P3HT Based Solar Cells

Sample of 22 Bulk Heterojunction Solar Cells



B. Minnaert and M. Burgelman 2007

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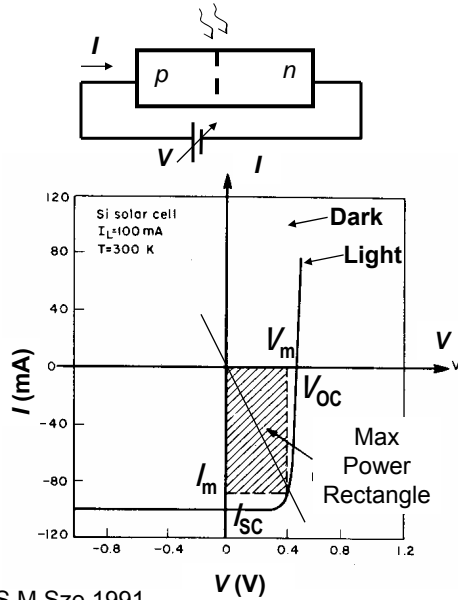
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Fill Factor

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Fill Factor Definition



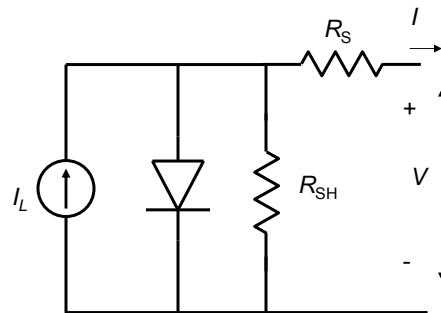
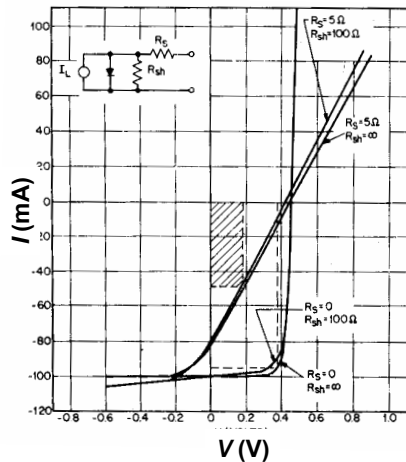
- Fill Factor FF is the ratio of area of maximum rectangle fitted in the 4th quadrant I - V and the product of V_{OC} and I_{SC}

$$\square FF = (V_m \cdot I_m) / (V_{oc} \cdot I_{sc})$$

S.M.Sze 1991

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Model for Solar Cells (Traditional)

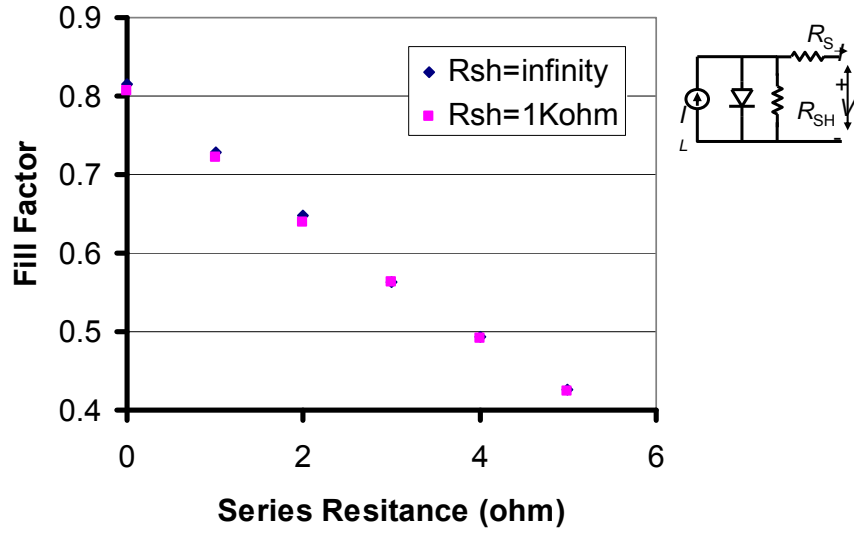


- Series resistance causes ohmic loss
- Shunt resistance causes charge separated to recombine

S.M.Sze 1991

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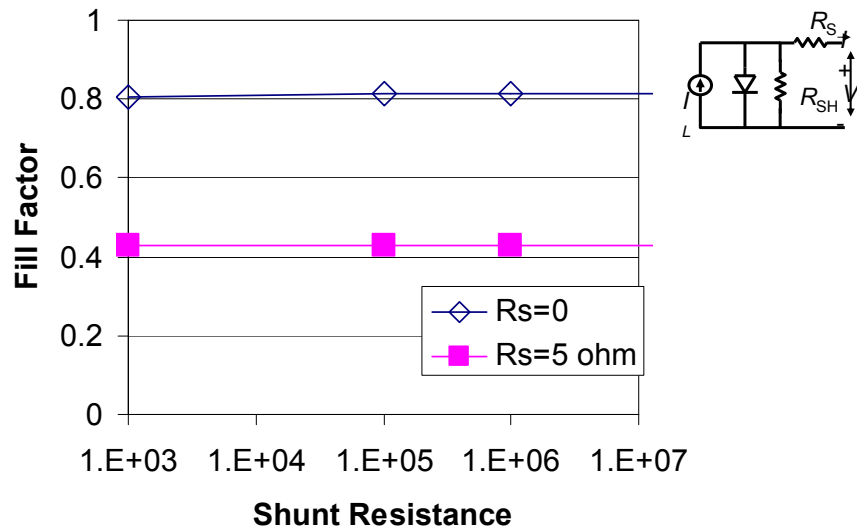
Variation in FF with R_s



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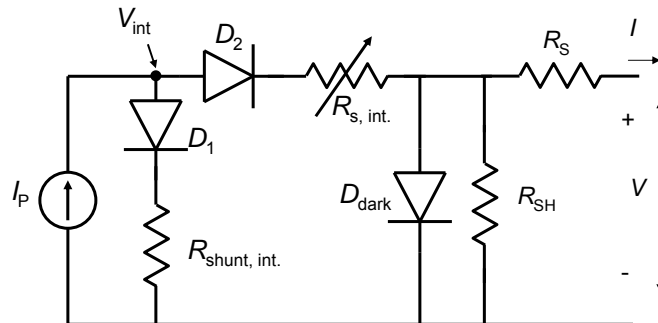
Variation in FF with R_{sh}



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Organic Solar Cell Model



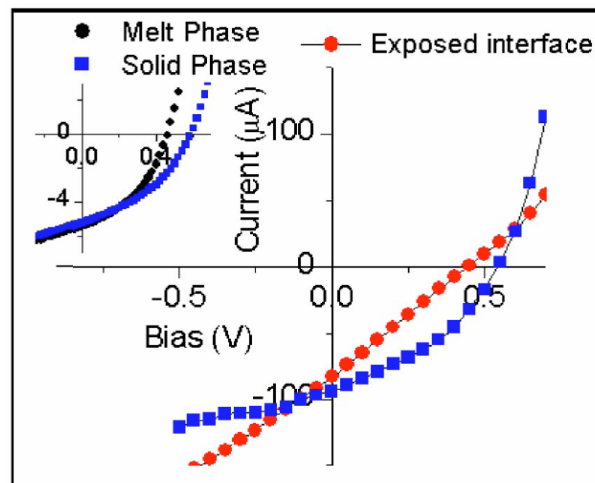
- I_L is a function of voltage
- Exciton generation I_p is a constant
- $R_{shunt, int}$ will account for exciton recombination
- $R_{s, int}$ will account for extraction of e^- and h^+ to electrodes

B. Mazhari 2006

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Contacts Effect Fill Factor



Gupta 2008

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We Discussed ...

- Calculating Efficiency of a Solar Cell
- Short Circuit Current
 - Quantum Efficiency
- Open Circuit Voltage
- Fill Factor

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